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ENGINEERING DEVELOPMENT ESTABLISHMENT

SKID STEERING OF WHEELED AND TRACKED VEHICLES - ANALYSIS WITH COULOMB FRICTION ASSUMPTIONS

BY

A.P. CREEDY

PUBLICATION EDE 38/84

Prepared and issued under my direction.

Brigadier Commander JAN 2 9 1985

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(TASK ARM 82/008)

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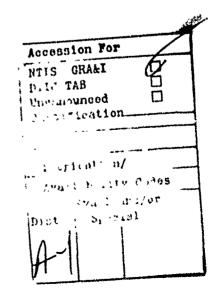
SUMMARY

Existing theoretical procedures for analysis of skid steering of wheeled and tracked vehicles have been extended to consider the interaction of forces generated for skid steering with the vertical loads carried at each wheel of the vehicle.

The developed theory has been organised into a system for numerical calculations of skid steering performance, which has been used to compare the predicted skid steering performance of a 6×6 wheeled vehicle, a 8×8 wheeled vehicle and a tracked vehicle with 12 road wheels.

The results indicated that the wheeled vehicles require greater 'track speed' difference and power input to maintain a steady turn than the tracked vehicle, and that the tracked vehicle can be expected to maintain its ability to steer over a wider range of slope angles and slope heading angles, than the wheeled vehicles. The 8×8 wheeled vehicle considered did not appear to offer any significant advantage, in terms of steering performance, over the 6×6 vehicle.

The results of the slope steerability calculations and, in the case of the 6×6 vehicle, comparison of calculated results with experimental data, indicated limitations to the developed theory which require further work to resolve.



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GLOSSARY PRINCIPAL USE OF SYMBOLS

A(J) (J = 1,2)	Non dimensional lateral (measured at right angles to vehicle centreline) coordinates of track ICRs relative to ground.
В	Non dimensional longitudinal (measured along vehicle centreline) coordinate of track ICRs relative to ground.
C(J) (J = 1,2)	Lateral coordinates of wheel/ground contact points, measured from vehicle centreline.
C(3)	Lateral coordinate of CG measured from vehicle centreline.
D4(I) (I = 1,N)	Deflection of suspension of Ith wheel from position at which zero force W1(I) is developed.
D6	Suspension deflection when radius arm angle is T7.
D7	Longitudinal component of vehicle weight acting through CG.
D8	Longitudinal inertia force acting through CG.
D9	Sum of D7 and D8.
DØ	Deflection of origin of chassis coordinate system from a position corresponding to zero deflection of each wheel suspension.
F1(I) (I = 1,N)	Longitudinal forces generated at the Ith wheel/ground contact point.
F3(J) (J = 1,N)	Track tension (tracked vehicles only).
F(J) (I = 1,N)	Longitudinal forces generated during sliding by entire 'row' of wheel/ground contact point.
G8	Slope heading angle.
G9	Roll angle of chassis, relative to ground.
Н	Height of CG above ground.
İ	Subscript used to label properties associated with the Ith wheel of an N-wheeled vehicle.
J	Subscript used to label properties associated with the left $(J = 1)$ or right $(J = 2)$ side of the vehicle.
K	Subscript used to label properties associated with the Kth pair of wheels of an N-wheeled vehicle, K = 1 denoting the front wheels.
K1(K)	Suspension deflection due to adjustment of suspension medium away from nominal position.

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C8 .	Slope heading angle.
G9	Roll angle of chassis, relative to ground.
H	Height of CG above ground.
I	Subscript used to label properties associated with the Ith wheel of an N-wheeled vehicle.
J	Subscript used to label properties associated with the left $(J=1)$ or right $(J=2)$ side of the vehicle.
К	Subscript used to label properties associated with the Kth pair of wheels of an N-wheeled vehicle, $K=1$ denoting the front wheels.
K1 (K)	Suspension deflection due to adjustment of suspension medium away from nominal position.

	
K.	Rolling resistance proportionality constant.
K ∢	Indicator for direction of rolling resistance forces. $K=-1$ corresponds to positive (forward) rolling resistance force, $K=-1$ to negative rolling resistance force.
K4	Tyre contact patch movement proportionality constant, as defined in equation (4-3).
[1	Track approach angle.
1,2	Track departure angle.
L(K)	Longitudinal coordinates of wheel/ground contact points. $L(N/2 + 1)$ is CG coordinate.
M ₁ })	Movement generated by longitudinal and lateral forces acting through vehicle CG.
м8	Coefficient of friction in transverse, or lateral, direction.
М9	Coefficient of friction in longitudinal direction.
M(J) (J = 1,2)	Sums of moments of lateral skid steering forces as defined by equation $(2-8)$.
MØ	Sum of moments of forces applied externally upon vehicle, about lateral centreline, as defined by equation (3-5).
N	Total number of wheel/ground contact points associated with a vehicle.
Nu	Power dissipated in longitudinal sliding of wheel/ground contact points.
N5	Power dissipated in lateral sliding of wheel/ground contact points.
N6	Power input to wheels assuming 100% transmission and regenerative efficiency.
P1(I) (I = 1,N)	Transverse force generated at the Ith wheel/ground contact point as a result of transverse sliding.
R	Madius of turn, measured at CG.
R2	Distance between centre of turn and vehicle centreline.
R6(I)	Motion resistance forces generated at the Ith wheel/ground contact point.
R8	Output/Input rotational speed ratio of driveline components enclosed within radius arm.
R9	Distance between centre of rotation of radius arm and centre of rotation of attached wheel.

C	X (4) (4) (4) (4) (4)
S	Steering ratio V1(1)/V1(2).
S(D4(I))	Functional relationship betwen suspension deflection $D4(I)$ and suspension force $W1(I)$ at the Ith wheel station.
T	Sum of T4 and T5.
T2(I)	Torque applied to Ith wheel.
Tч	Transverse component of vehicle weight, acting through vehicle CG.
T5	Transverse inertia force acting through vehicle CG.
т6	Yaw angle - angle between vehicle centreline and direction of motion of CG.
Т7	Radius arm angle when suspension deflection is D6.
T8(I)	Angle of Ith radius arm with respect to datum on chassis.
Т9	Chassis roll angle.
V	Velocity of vehicle measured at CG.
V1(I) (J = 1,2)	Velocities of each 'track' or row of wheel/ground contact points relative to the vehicle.
V2(J) (J = 1,2)	Velocities of each 'track' relative to the ground, resolved parallel to the longitudinal centreline of the vehicle, or slip velocities.
V3(J) (J = 1,2)	Velocities of the vehicle hull at the track attachment points, resolved parallel to the longitudinal centreline of the vehicle.
VØ	Velocity of vehicle measured along vehicle centreline.
W(I)	Vertically upward force applied at the Ith wheel/ground contact point.
W1(I)	Vertically downward force applied by the supension at the Ith wheel/ground contact point.
W2(I)	Vertically downward force applied at the Ith wheel/ground contact points as a result of the generation of propulsive and skid steering forces.
W3	Vertical component of vehicle weight acting through CG.
W4	Vehicle weight, acting through CG.
W9	Wheel diameter.

Tyre contact patch movement in a forward direction, due to torque transmitted to wheel.

Z(K) Indicator for direction of radius arms on wheeled vehicle (K = 1, N/2) Z(K) = -1 denotes 'leading' radius arm, Z(K) = +1 denotes trailing radius arm.

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ANALYSIS WITH COULOMB FRICTION ASSUMPTIONS

(TASK ARM 82/008)

by

A.P. CREEDY

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- A. Skid Steering by K.R. Weiss (Automobile Engineer April 1971)
- B. A Theoretical Analysis of Steerability of Tracked Vehicles by M. Kitano and H. Jyozaki
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 An Interim Report on the Operations of TV1000.
 FVRDE Report No BR 189 dated 1 June 1966.

INTRODUCTION

- 1. Skid steering has been widely applied to track laying vehicles such as bulldozers and current main battle tanks. Tracks are insufficiently flexible in a lateral direction to permit them to be laid on the ground in curves corresponding to a practical radii of turn. Instead, the propulsive force applied by one track is increased relative to the other until the vehicle is forced to slew in the desired direction. Basic theory for skid steering of tracked vehicles has been published (Ref C) and introduces analysis of the forces acting upon the track during skid steering.
- 2. In military track laying vehicles, the use of skid steering has a useful byproduct in that the tracks and suspension do not consume a large proportion of the internal volume of the vehicle. Wheeled vericles have certain herent advantages, automotively, over 'equivalent' tracked vehicles including the ability to travel fast over smooth ground for a relatively lower power input. Wheeled and tracked vehicles have both advantages and disadvantages in particular applications but it is not the aim of this document to examine all of these. A wheeled vehicle may well be a viable competitor to a tracked vehicle for a particular application, and pressure to maximise use of internal volume, together with other considerations, can result in consideration of a skid steered wheeled concept.

- 3. Skid steering of a wheeled vehicle can be achieved by increasing the total torque driving the row of wheels on one side of the vehicle relative to the torque supplied to the other row of wheels, until the vehicle is forced to slew. During skid steering, the rotational speed of the wheels in one line or row will increase relative to the other row, but normally the transmission arrangement imposes equal rotational speed on all wheels within a row.
- 4. Theory applying to skid steering of wheeled vehicles has been published (Ref A). Few skid steered wheeled military vehicles have been built to date, and data on their steering performance is insufficient for making informed comparisons with existing vehicles.

AIM

5. The aim of the work documented here was to make use of skid steering theory to predict the steering characteristics of wheeled skid vehicles, and to compare these with the steering characteristics of tracked vehicles predicted by similar theory. Where possible, the results of theoretical predictions are compared also with experimental data.

BASIC PRINCIPLES AND ASSUMPTIONS

Limitations of Theory

- 6. The existing theory (Ref A) for wheeled vehicles has the following limitations:
 - Vehicle motion on flat hard ground at constant speed only is considered.
 - b. Wheels are laterally and longitudinally rigid, and contact the ground at a single point. Forces generated by sliding of these points relative to the ground is governed by coulomb friction laws.
 - c. Lateral and longitudinal forces may be applied at the vehicle CG, but lateral forces only are considered when calculating the vertical load caried by each row of wheels. Equal vertical loads are assumed to be carried by each wheel within a row.
 - d. The effects of the following upon the vertical load carried by each wheel are not considered:
 - (1) Suspension flexibility.
 - (2) Vertical forces generated at each wheel which are a function of torque transmitted, and the specific driveline and suspension arrangement.
 - e. The theory deals with a 6 wheel vehicle with symmetrical wheel spacing and CG position fixed in a horizontal plane

- The theory has been extended within this document and attempts to to overcome the last three limitations at c, d and e above, by considering an N-wheeled vehicle (N may be set to N or any greater number divisible by 2) where effects on individual wheel loads due to wheel suspension characteristics, variable positioning of the CG in three dimensions, forces applied at the CG, unequal wheel spacing, and vertical forces caused by torque transmitted to each wheel are calculated. The longitudinal flexibility of the tyres is partially considered by application of rolling resistance forces at each wheel, proportional to the load carried, and by introducing a longitudinal movement of the wheel/ground contact point proportional to the torque being applied to the wheel.
- 8. The theory developed in this document does not deal with the most significant of the limitations, a and b above, the non applicability to motion on soft ground, and the overall effects of tyre flexibility. These limitations remain for future resolution.
- 9. As detailed within this document, the theory as developed can be applied to tracked vehicles, due allowance being made for the different way in which track tension will modify the fraction of vehicle weight caried by each road wheel. When modified for tracked vehicles, the theory developed here becomes similar to that given in Ref B.
- 10. Within this document, the symbol I has been used to refer to the Ith wheel, (I = 1 to N), J to the Jth row of wheels (J = 1, 2 with 1 referring to the row on the outside of the turn) and K to the Kth "axle" or pair of wheels (K = 1, N/2). For given values of J and K, I = N/2 * (J-1) + K. Where mathematical relationships stated in this document have been used directly in the computer programs used for skid steering calculations, the style of variable name imposed by the BASIC programming language used has, were practicable, been retained.

Note: Throughout this document all figures referenced are figures of Annex D

Instantaneous Centres of Rotation

- 11. Figure 1 shows the essential details of a hypothetical N-wheeled (N \times N) vehicle. Wheels within each row are inter connected to run at the same speed. The N/2 points on the underside of the wheels of one row which are in contact with the ground will therefore behave, instantaneously, as a single rigid body, or as a 'track' which is in contact with the ground at N/2 points. The term 'track' is used within this report to denote the N/2 contact points of a row of wheels.
- 12. Figure 2 shows forces applied to the vehicle in the plane of the wheel/ground contact points, as a result of sliding of the contact points relative to the ground. The vehicle is making a turn to the right, about a point not shown on Fig 2. The left hand 'track', in order to generate forward frictional forces f1 and lateral forces P1 as shown sliding rearwards relative to the ground as well as rotating clockwise with the vehicle. Since the 'track' behaves as a rigid body, it rotates about a single point on the ground, in this case 03 as shown on Fig 2, the Instantaneous Centre of Rotation (ICR) of the 'track' relative to the ground. For the left hand 'track', 03 is located relative to the vehicle by B and A (1), for the right hand track, the ICR at 02 is defined by B and

- A (2). The actual dimensions of the ICR coordinates are A(1)*L(1), A(2)*L(1), B*L(1) where L(1) is a characteristic vehicle dimension.
- dimensional kinematics provides that the relative instantaneous centres of three rigid bodies in relative motion lie on a straight line. Taking these three bodies as the vehicle, the less hand 'track' and the ground, referring now to Fig 3, the ICR of the vehicle relative to the ground is the centre of turn 01, the ICR of the 'track' relative to the vehicle is at infinity (since the track does not rotate relative to the vehicle) on a line at right angles to WZ, therefore the ICR of the 'track' relative to the ground lies on a line between 01 and infinity, which is at right angles to WZ. An identical argument applies to the right hand 'track'. Therefore both ICR 02 and 03 lie on a line through 01 which is at right angles to WZ. The coordinates of 02 and 03 in the longitudinal direction are identical, and defined by B. The lateral coordinates of the ICR of the tracks relative to the ground are defined as shown in Fig 2 and Fig 3 by A(1) and A(2), which are not necessarily equal.
- 14. The values of A(J) are defined as positive when associated with positive (sliding rearwards) slip velocity of the wheel/ground contact points. In the case illustrated in Fig 2 and 3, A(2) has a negative value. Determination of the location of the two 'track' ICRs will establish the direction of sliding of each contact point, and enable each force F1(I), P1(I), (I = 1, N) to be calculated. Calculation of A(1), A(2) and B is covered in para 23 to 39.

11

Radius of Turn

- 15. Figure 3 shows a skid steered vehicle in a steady turn about a centre of turn 01 such that the CG follows a circular path of radius R, at peripheral speed V. R is defined as the radius of turn, and V the total speed of the vehicle, and these are normally required as input data for the calculations described.
- 16. VO is the component of vehicle velocity along the longitudinal centreline through 0. Its value is constant at VO at all points along the centreline, including the point of intersection of the centreline with the line joining 01 with the two 'track' ICR 02 and 03. VO is defined as the 'forward speed' of the vehicle.
- 17. The angle between the cirections of V and VO is defined on the yaw angle T6. The following relationships apply:

T6 =
$$Sin^{-1}$$
 ((B*L(1) - L(N/2 + 1))/R) - (1-1)
V0 = V * Cos (T6) - (1-2)
R2 = R * Cos (T6) - C(3) - (1-3)

The inertia forces acting at the CG are given by:

$$D8 = W4 * V^2/(R*g) * Sin (T6) - (1-4)$$

 $T5 = W4 * V^2/(R*g) * Cos (T6) - (1-5)$

where W4 is the mass of the vehicle.

Slip Velocities and Steering Ratio

- 18. The triangular construction of Fig 4, based upon the line through 01, 02 and 03 which is at right angles to the longitudinal centreline of the vehicle, provides useful relationships between key velocities. The velocities are (for J = 1, 2):
 - V1(J) Velocities of 'tracks' relative to the vehicle.
 - V2(J) Velocities of 'tracks' relative to the ground resolved parallel to the longitudinal centreline of the vehicle, or slip velocities.
 - V3(J) Velocities of the hull at the track attachment points, resolved parallel to the longitudinal centreline of the vehicle.
- 19. The triangular nature of the construction joining V3(1), V0 and V3(2) will be obvious from consideration of rotation of the vehicle about 01. The case for erection of the velocities V1(1) and V1(2) at 03 and 02 is less obvious. Consider two outriggers of length A(1)*L(1), one attached to the hull at A, the other attached to the 'track' at A, both initially in the position A-03. All points in the two outriggers will diverge at velocity V1(1). However, since 03 is the ICR of the 'track' relative to the ground, the extremity of the outrigger attached to the 'track' will be instantaneously at rest above point 03, and the outrigger attached to the hull, rotates with the hull about 01 and its extremity moves away from point 03 with velocity V1(1). A similar argument applies to V1(2). The construction of V2(J) follows from the relationship:

$$V2(J) - V1(J) - V3(J)$$

20. The steering ratio S is defined as the ratio V1(1)/V1(2) and is equal to the ratio of outer/inner wheel rotational speed. From Fig 4:

$$S = (R2 + C(1) + A(1) + L(1))/(R2 + C(2) + A(2) + L(1)) - (1-6).$$
 $V1(1) = V0 + (1 + C(1)/R2 + A(1) + L(1)/R2)$
 $V1(2) = V1(1)/S$
 $V2(J) = A(J) + L(1) + (S + V1(2) - V1(2))/$
 $(C2 + A(1) + L(1) - A(2) + L(1))$
 $(C2 + A(1) + L(1) - A(2) + L(1))$
 $(C3 + A(1) + L(1) - A(2) + L(1))$

where C2 - C(1) - C(2) - wheel track.

21. Figure 5 shows a small radius turn being generated by a negative steering ratio. A 'pivot' turn is defined here as a turn with S = -1, and provided that A(1) = A(2), this will result in the centre of turn lying on the longitudinal centreline of the vehicle.

Slope Operation

22. Figure 6 shows the envelope of wheel/ground contact points WXYZ standing on a slope ABCD which is at an angle T3 to the horizontal. The vehicle is pointing in a direction defined by angle G8, measured in plane ABCD. G8 is referred to as the slope heading angle. The vehicle is turning right, or up the slope. The vehicle weight W4 is resolved into a force W3 normal to plane ABCD, and forces T4 and D7 in the lateral and

longitudinal directions of the vehicle, all acting through the vehicle CG. The following relationships apply:

$$W3 = W4* Cos (T3)$$
 - (1-10)
 $T4 = W4* Cos (G8)* Sin (T3)$ - (1-11)
 $D7 = W4* Sin (G8)* Sin (T3)$ - (1-12)

DETERMINATION OF INSTANTANEOUS CENTRE OF ROTATION (ICR)

FOR EACH ROW OF WHEELS, OR "TRACK", RELATIVE TO THE GROUND

Forces Acting at Wheel/Ground Contact Points

- 23. Figure 2 shows the positions of the wheel/ground contact points of a N x N vehicle relative to a L (length), C (width) coordinate system having origin 0, and + ive L and C in the directions shown. The contact points of the four corner wheels are at W, X, Y, Z and the coordinates of the Ith contact point is L(K), C(J). The contact points are axially symmetrical, C(1) = -C(2) and L(1) = -L(N/2).
- 24. As shown in para 13, the ICR coordinates for each row of contact points lie on a line at right angles to the vehicle centreline. For consistency with earlier work, the distance of this line from 0 is defined as a multiple B of the vehicle semi length, or B^* L(1). The distance of each ICR from the relevant row of wheels is defined as a multiple A(J) of the vehicle semi length or A(J)* L(1) (J = 1, 2).
- 25. The transverse and longitudinal (forward propulsive) forces generated by the sliding of each wheel/ground contact point about 01 or 02 are P1(I) and F1(I) respectively. (I = 1 to N). If the vertical load at each contact point is W(I) and the wheel/ground coefficients of (coulomb) friction in the transverse and longitudinal directions are M8 and M9 respectively, use of Micklethwaite's suggestion (see Ref A and Ref C) leads to the following equations for F1 and P1. For I = 1 to N:

F1(I) = M8* W(I)* Cos (
$$\Theta$$
(I)) - (2-1)
P1(I) = -M9* W(I)* Sin (Θ (I)) - (2-2)

the negative sign has been introduced in equation (2) in order to make transverse forces acting at the wheel/ground contact points positive when in the direction of the centre of turn, which in this case is the direction 01 - 02. Forces F are positive in the direction of motion of the vehicle.

26. The geometry of Fig 2 leads to the following expressions for cos 0 and sin 0:

Note that for the situation shown in Fig 2, for J=1 (the 'outside' row of wheels), all cos 0 are >0 and sin 0 <0 for K=2 to N/2. For J=2 (the 'outside' row of wheels), all cos 0 are <0 and sin 0 <0 for

K=2 to N/2. Forces R6(I) (I = 1 to N) act at each contact point in a direction opposing forward (Parallel to OL) motion of the relevant row of wheel hubs over the ground. Their sum is the "rolling resistance" of the vehicle.

27. In accordance with the sign convention for longitudinal forces given above, the forces R6 as depicted in Fig 1 and 2 are negative. This is consistent with all wheels rolling in a 'forward' direction which is normally the case despite the forward sliding of the inside (right hand) row of contact points. The forces R6 are therefore assumed to oppose the direction of motion of each side of the vehicle hull parallel to OL and further assumed to have a magnitude proportional to the vertical load carried by the wheel such that:

$$R6(I) = -K2*W(I)$$
 (I = 1 to N)

where K2 is a suitable constant.

28. In the case of a pivot turn (normally the only practical case where hull velocities V3(J) are of unequal sign) the right hand row of wheels shown in Fig 2 would have positive (forwards) forces R6(I) (I = N/2 + 1 to N) acting at the contact points. Within the computer programs based upon the theory of this report the following expression was used for R6. For I = 1 to N:

$$R6(I) = -K2*K3*W(I)$$
 - (2-5)

where K3 = +1 for all conditions except a pivot turn, when K3 = -1 for J = 2 only.

29. If F(J), J=1, 2 are the total longitudinal forces generated by the outer and inner 'tracks' respectively, and P(J), J=1, 2 are the transverse forces:

$$F(J) = \sum_{K=1}^{N} (F1(I) + R6(I))$$

$$P(J) = \sum_{K=1}^{N} P1(I)$$

30. Using equations (2-1) to (2-5) the above expressions can be re-written:

$$F(J) = M8 \sum_{K=1}^{N} W(I) * Sin \Theta(I) - K2 \sum_{K=1}^{N} K3 * W(I) - (2-6)$$

$$\frac{N}{2}$$

$$P(J) = -M9 \sum_{K=1}^{N} W(I) * Cos \Theta(I) - (2-7)$$

31. The transverse forces applied at each contact point apply a moment, opposing the turn, to each row of wheels. If M(J) (J = 1, 2) are the moments applied to each row of wheels, and defining positive moments as anticlockwise in the plane of Fig 2, then:

$$M(J) = -\sum_{K=1}^{N} P1(I) * L(K)$$

$$K = 1$$

$$M(J) = M9 \sum_{K=1}^{N} L(K) * W(I) * Sin \Theta (I) - (2-8)$$

Vehicle Equilibrium

32. Figure 2 shows all forces acting in the plane of the ground upon the vehicle at the wheel/ground contact points. Fig 1 is an isometric view of the simplified vehicle considered by this analysis, in which all externally acting forces, including those of Fig 2, are shown.

The additional forces are:

- D9 A rearward longitudinal force acting through the vehicle CG. In a steady turn as considered by this analysis, this will normally be the sum of an inertia force (D8) opposing accelleration of the CG in the forward direction and a component of vehicle weight (D7) acting in a rearward direction, due to the vehicle standing on a slope.
- T A lateral (or transverse) force acting through the vehicle CG. It is the sum of an inertia force (T5) and component of vehicle weight (T4) acting in parallel to OC, away from the centre of turn.
- W3 A component of vehicle weight (W4) acting normally to the plane of the ground (WXYZ).
- 33. The additional forces D9, T, W3 are positive in the directions shown on Fig 1. If the CG of the vehicle is offset from 00" (Fig 1) by L (N + 1), C(3) measured in the L, C coordinate system, forces T and D9 will generate a moment M(3) about 00" as follows:

$$M(3) = D9 + C(3) + T + L(N/2 + 1)$$
 - (2-9)

34. In a turn of constant vehicle speed and radius, the forces shown on Fig 1 will be in equilibrum. Three equations defining this equilibrum are:

(Equilibrum of moments about 0)")

$$M(1) + M(2) + M(3) - (F(1) * C(1) + F(2) * C(2)) = 0 - (2-10)$$

(Equilibrum of longitudinal forces)

$$F(1) + F(2) - D9 + 0$$
 - (2-11)

(Equilibrum of lateral forces)

$$P(1) + P(2) - T = 0$$
 - (2-12)

where M, F and P are defined by equations (2-6), (2-7), (2-8), (2-9).

- 35. It is required to solve (2-10), (2-11), (2-12) for A(1), A(2) and B for given values of L(K), C(J), W(I), M8, M9 and K2. A numerical method as follows has been found to give single solutions for A(1), A(2), B.
- 36. For given conditions as stated, the left hand side of equations (2-10), (2-11), (2-12) are treated as functions of A(1), A(2) and B only. Detonating these functions as P2, G2, R2 respectively, if $(A(1))_1$, $(A(2))_1$ and $(B)_1$ are approximate (guessed) solutions, and subject to errors Δ A(1), Δ A(2), Δ B, then:

P2 (((A(1)),
$$+ \Delta \hat{A}^{(1)}$$
), ((A(2)), $+ \Delta A(2)$), ((B), $+ \Delta B$) $+ O$ - (2-13)

$$G2 ("""") = 0 - (2-14)$$

37. Expressing the left hand sides of 13, 14, 15 as the first terms of the Taylor series of P2, G2 and R2 gives:

$$(P2)_1 + \Delta A(1) \left[\frac{\partial P2}{\partial A(1)} \right]_1 + \Delta A(2) \left[\frac{\partial P2}{\partial A(2)} \right]_1 + \Delta B \left[\frac{\partial P2}{\partial B} \right]_1 = 0 \qquad - (2-16)$$

$$(G2)$$
, $+\Delta A(1)$ $\left[\frac{\partial G2}{\partial A(1)}\right]$ $+\Delta A(2)$ $\left[\frac{\partial G2}{\partial A(2)}\right]$ $+\Delta B$ $\left[\frac{\partial G2}{\partial B}\right]$ $(2-17)$

$$(R2)_{1} + \Delta A(1) \left[\frac{\partial R2}{\partial A(1)} \right]_{1} + \Delta A(2) \left[\frac{\partial R2}{\partial A(2)} \right]_{1} + \Delta B \left[\frac{\partial R2}{\partial B} \right]_{2} = 0 \qquad -(2-18)$$

Suffix 1 denotes evaluation of the relevant function at the points $(A(1))_1$, $(A(2))_1$, $(B)_1$.

38. By treating approximations (2-16), (2-17), (2-18) as equalities, the errors $\Delta A(1)$, $\Delta A(2)$, ΔB become approximate errors and can be found by solving (2-16), (2-17), (2-18) using standard methods for simultaneous linear equations.

Hence:

$$\Delta A(1) = D1/D$$

$$\Delta A(2) = D2/D$$

where D =
$$\begin{bmatrix} \frac{\partial P2}{\partial A(1)} \end{bmatrix}_1$$
, $\begin{bmatrix} \frac{\partial P2}{\partial A(2)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial B} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial G2}{\partial A(1)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial G2}{\partial A(2)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial G2}{\partial B} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial R2}{\partial A(1)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial R2}{\partial A(2)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial B} \end{bmatrix}_1$, $\begin{bmatrix} -(P2)_1 \end{bmatrix}$, $\begin{bmatrix} \frac{\partial P2}{\partial A(2)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial B} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial A(2)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial B} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial A(1)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial A(1)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial A(2)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial B} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial A(1)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial A(2)} \end{bmatrix}_1$, $\begin{bmatrix} \frac{\partial P2}{\partial$

39. Improved estimates $(A(1))_2$, $(A(2))_2$ and $(B)_2$ are found from:

$$(A(1))_2 = (A(1))_1 + \Delta A(1)$$

 $(A(2))_2 = (A(2))_1 + \Delta A(2)$
 $(B)_2 = (B)_1 + \Delta B$

these improved estimates are sufficiently accurate if $(P2)_2$, $(G)_2$ and $(R2)_2$ are all sufficiently close to zero. If not, the process is repeated using $(A(1))_2$, $(A(2))_2$, $(B)_2$ as the new guessed solutions. This procedure has been found to be consistently convergent in situations where solutions are possible. For evaluation of the terms containing partial derivatives, see Annex A.

DERIVATION OF INDIVIDUAL WHEEL LOADS

- 40. Figure 7 is developed by assuming that the plane PQRS is parallel to plane WXYZ (ground level), fixed to the vehicle chassis and contains a two dimensional coordinate system such that 00^{1} = H1 with major axes parallel to those of the coordinate system in plane WXYZ. It is also assumed that each wheel of the vehicle is attached to the chassis via a suspension system which applies downward forces W1(I) (I = 1 to N) at the Ith wheel which is a function S of the vertical movement D4(I) (I = 1 to N) of the wheels relative to the chassis from an unloaded position.
- 41. "Vertical" is defined as parallel to 00¹, and the chassis pitch and roll angles T9 and G9 are assumed to be sufficiently small, such that, errors in assuming that wheel deflections D4(I) always take place in a vertical direction can be neglected.
- 42. The CG of the vehicle chassis is assumed to lie on plane PQRS when all suspension deflections are equal to K1(K). K1(K) is a distance associated with each wheel pair or axle, and is defined as the vertically downward movement of an unloaded wheel resulting from adjustment of the suspension relative to the chassis, away from a position which places the wheel/ground contact point of the unloaded wheel in plane WXYZ when 00^{1} = H1.
- 43. Wheel loads were adjusted during the course of testing TV1000, as reported in Ref D, by adjusting the positions of suspension spring anchorages relative to the chassis. This effect was modelled by introducing K1(K). Values of K1(K) for TV1000 were not given, but estimated values were found by trial and error, as described in Para 83. Normally, all K1(K) = 0, ie the wheel/ground contact points of unloaded wheels lie in a single plane, normally parallel to a suitable reference plane on the chassis.
- The coordinate system created in plane PQRS is considered to be fixed to the vehicle chassis. When forces W3, D9 and T are applied at the CG position, points in plane PQRS vertically above the wheel/ground contact points in plane WXYZ will adopt new positions in plane P'Q'R'S' as shown in Fig 3. The vertical movement of these points will be equal to the vertical movement of the wheel/ground contact points relative to the chassis, D4(I).
- 45. The suspension deflections are given by:

$$D4(1) = D0 + L(K) Sin (T9) + C(J) Sin (G9) + K1(K) - (3-1)$$

The height H of the CG above plane WXYZ is:

$$H = HI - (DØ + L(N/2 + 1) Sin (T9) + C(3) Sin (G9) - (3-2)$$

where L(N/2+1) and C(3) are the coordinates of the CG in the system attached to the chassis. Generally, L(N/2+1) and C(3) are small and DØ does not vary greatly. H was treated as constant within the calculations described below.

46. Certain arrangements for driving the wheels can cause forces W2(I) to be applied to the Ith wheel, independently of the suspension forces W1(I). Both W1(I) and W2(I) are considered to act vertically downwards. If the vertically upward force acting at the Ith is W(I) then (as shown in part. 58 to 71):

$$W(I) + W1(I) + W2(I)$$
 - (4-6)

- 47. Paragraphs 58 to 71 contain the derivation of W2(I) for radius arm suspension and drive arrangements typical of those proposed for wheeled skid steered vehicles, as well as the derivation of W2(I) for tracked vehicles.
- 48. If the function S {D4(I)} relating D4(I) and W1(I) is linear, considerations of vehicle equilibrium leads to N linear equations which can be solved by matrix methods to provide the wheel loads W(I) directly, for given values of W2(I). However this approach could not be used for non linear S, which is a probable feature of a suspension designed for fast off road rovement.
- 49. The following method of calculating DØ, T9 and G9 from considerations of vehicle equilibrium uses on Newtons iteration in the same way as the method used in para 11 to 15 to calculate ICR coordinates. The method ultimately depends on evaluation of the suspension force S $\{D4(I)\}$ and spring rate $3S\{D4(I)\}$ for

given values of deflection D4(I) being possible. Some suspension characteristics may require the use of data fitting (curve fitting) techniques in order to achieve this in a convenient manner, and a method used is described in Annex B.

50. Referring to Fig 1, denoting the moments of all externally applied forces acting about XY, WZ and OC As M(1), M(2) and MØ respectively:

$$\frac{N}{2}$$

$$M(1) = \sum_{i=1}^{N} W(1)^{i} (C(1) - C(2)) - T*H - W3* (C(3) - C(2)) - (3-3)$$

$$M(S) = \sum_{i=1}^{N} W(i) * (C(2) - C(1)) - T*H + W3* (C(1) - C(3)) - (3-4)$$

$$\frac{N}{2}$$
MØ = $\sum_{K=1}^{N} (W(K) + W(N/2 + K)) \times L(K) + D1 \times H - W3 \times L(N + 1) - (3-5)$

- 51. In the case of (3-3) and (3-4), positive moments are considered to be anticlockwise viewing in the direction LO. C(2) is normally negative. The effect of chassis pitch and roll angles on the projection of distances C(3) and L(N+ 1) onto plane WXYZ has been neglected.
- 52. It is required to find DØ, T9 and G9 such that M(1), M(2) and MØ are each close to zero. Equation (19) can then be used to find the

suspension deflections D4(I) and hence the suspension forces W1(I). The Wheel loads are then calculated using (4-6).

- 53. Initial values $(M(1))_1$, $(M(2))_1$, $(M\emptyset)_1$, are computed using initial estimates of $(D\emptyset)_1$, $(G9)_1$, and $(T9)_1$ via equations $(3-1)_1$, (4-6) and the functional relationship betwen W1(I) and D4(I). The initial estimates are normally $(G9)_1 = (T9)_1 = \emptyset$ and $(D\emptyset)_1$ set to the value of suspension deflection obtained for a suspension force of W3/N. Forces W2(I) will have been computed separately and are treated as known constants within this section. (See "Overall Method of Computation" para 75 to 77).
- 54. If $\Delta D\emptyset$, $\Delta T9$ and $\Delta G9$ are approximate errors in $(D\emptyset)_1$ $(T9)_1$ $(G9)_1$ then:

$$(M(1))_1 + \Delta D\emptyset \left[\frac{\partial M(1)}{\partial D\emptyset}\right]_1 + \Delta T9 \left[\frac{\partial M(1)}{\partial T9}\right]_1 + \Delta G9 \left[\frac{\partial M(1)}{\partial G9}\right]_1 = 0$$
 - (3-6)

$$(M(2))_1 + \Delta D\emptyset \left[\frac{\partial M(2)}{\partial D\emptyset}\right]_1 + \Delta T9 \left[\frac{\partial M(2)}{\partial T9}\right]_1 + \Delta G9 \left[\frac{\partial M(2)}{\partial G9}\right]_1 = 0 - (3-7)$$

(MØ), +
$$\Delta$$
DØ $\left[\frac{\partial M}{\partial D}O\right]_1$ + Δ T9 $\left[\frac{\partial T}{\partial M}O\right]_1$ + Δ G9 $\left[\frac{\partial G}{\partial G}O\right]_1$ = 0 - (3-8)

where 1 denotes evaluation of the relevant function at the point $(D\emptyset)_1$, $(T9)_1$, $(G9)_1$.

- Provided that the terms containing partial derivatives can be evaluated, the approximate errors can be found by solving the three linear equations (3-6), (3-7), (3-8) by methods identical with those used in Part 1. For evaluation of the terms containing partial derivatives, see Annex C.
- 56. Improved estimates of DØ, T9, and G9 are then obtained:

$$(DØ)_2 = (DØ)_1 + \Delta DØ$$

 $(T9)_2 = (T9)_1 + \Delta T9$
 $(G9)_2 = (G9)_1 + \Delta G9$

this process is repeated until the values obtained for M(1), M(2), M0 by substitution of the improved estimates of D0, T9, G9 into equations (3-1), (3-3), (3-4), (3-5) are sufficiently close to zero.

57. The speed of the method depends on the accuracy of the initial estimates of DØ, T9, G9. If significant forces T and D9 are applied to the vehicle, the wheel loads are far from equal and the first estimates for DØ, T9, G9 on the basis given above are inaccurate. Under these conditions, the iterative process requires several passes to reach equilibrium.

EFFECT OF SUSPENSION AND FINAL DRIVE ARRANGEMENTS ON

WHEEL LOADS

Wheeled Vehicle

- 58. Figure 8 shows a suspension arrangement typical of proposed and actual wheeled skid steered vehicles. A radius arm is attached to the vehicle at 0 and can rotate relative to the hull about 0. Concentric with the radius arm attachment at 0 is an input drive shaft which is part of the radius arm and is connected to an output shaft at A by mechanisms internal to the radius arm such as gears or a chaindrive, normally such that the input and output shaft rotate in the same direction. The wheel can rotate about A relative to the radius arm and is driven by the output shaft.
- 59. Torque M_S is shown being applied to the radius arm (not the concentric drive shaft) at 0 by the suspension medium. This torque can be replaced by a downward load W1(I) applied to the radius arm at A such that:

$$W1(I) = M_g/(R9^{\hat{N}} \cos (\tilde{T}8\%I)) \qquad \qquad - (4-1)$$

- 60. In practice a pure torque is applied to the radius arm at 0 only if the suspension medium is inhoard of point of attachment to the hull. Outboard suspension components (Gas strut, coil spring, etc) could be attached to the radius arm anywhere between 0 and A. In all cases, a moment M_S about 0 is generated and the equivalent downward force W1(I) at A can be obtained from (4-1). Generally (and within the calculations described in Fara 40 to 57) suspension force/deflection characteristics are given in terms of the vertical force W1(I) for a given vertical deflection at A of D4(I).
- 61. Torque T_{IN} is shown being applied to the input drive shaft by the vehicle driveline with torque T2(I) being applied to the output drive shaft at A. The forces W(I) (vertical load), F1(I) (forward propulsive force) and R6(I) (resistance to forward motion) are transmitted onto the end of the radius arm at A, via the wheel. The wheel has torque T2(I) applied to it by the output shaft.
- Deformation of the tyre in forward motion is considered to result in a forward movement x of the contact point as shown. It is proposed that x is dependent on the input torque T2(I) as follows:

 $x = x_0 + T2(I)/K4$ where K4 is constant, and $x = x_0$ when T2(I) and F1(I) are zero. Hence from consideration of wheel equilibrium with T2(I) = F1(I) = 0:

$$x_0 = -\frac{W9 \times R6(I)}{2 \times W(I)}$$
 (ie x_0 is + ive for rearward $R6(I)$)

equilibrium of the wheel with non zero values of T2(I) and F1(I) gives:

$$T2(I) = W(I) \times x - (F1(I) + R6(I)) \times W9/2 = \emptyset$$
 - (4-2)

or
$$T2(I) - W(I) + (x_0 + T2(I)/K4) - (F1(I) + R6(I)) + W9/2 = \emptyset$$

substituting for xo:

$$T2(I) = F1(I) \times (W9/(2 \times (1 - W(I)/K4)))$$
 - (4-3)

a value for K^{ij} was estimated from data published in Ref D for TV1000 when climbing slopes. The value was K^{ij} = 65400. This results in a value of x equal to 0.157 feet for T2(I) = 7000 ft lb, and would apply to the tyres specific to TV1000 only. (See para 89 - TV1000 - Tyre Contact Point Movement, for this derivation of K^{ij} .)

63. Consider equilibrium of the radius arm in Fig 8:

$$T_{IN} = T_{2}(I) = M_{s} + W(I) + R_{9} + Cos(T_{8}(I)) = (F_{1}(I) + R_{6}(I)) + (R_{9} + S_{10} + (T_{8}(I)) = \emptyset$$

substituting for M_S and T2(I) from (4-1) and (4-2):

$$W(I) = W(I) = (F(I) + RG(I)) \times TAN (TB(I))$$

$$+ F1(I) \times W9 \times (1-R8)/(2 \times (1-W(I)/K4) \times R9 \times Cos(T8(I)) - (4-4)$$

where $R8 = T_{IN}/T_2(I)$, equal to the speed reduction ratio of the radius arm assuming 100% transmission efficiency.

64. It can be seen from (4-4) that for $T8(I) \neq 0$ and/or $R8 \neq 1$, that $W(I) \neq WI(I)$. If a positive difference that exists between W(I) and WI(I) is considered to be a downward force W2(I) acting at A, then:

$$W(I) = W1(I) + W2(I)$$
 - (4-5)

W2(I) would therefore appear on the left hand side of equation (4-4).

65. "Leading" as opposed to "trailing" radius arms imply 290° < T8(I) < 90° , in which case W2(I) will normally be negative, or in an upward direction. For a radius arm angle of (180 - T8(I)), equation (4-4) provides an identical absolute value of W2(I), the sign being changed. A term Z(K) (K = 1 to N/2) is introduced in (4-4) which is set to -1 or +1 depending on whether the radius arm 'leads' or 'trails' (as in Fig 9). Radius arm angles are then always measured as the smallest angle from horizontal. (4-4) becomes:

$$W2(I) = Z(K) \times ((F1(I) + R6(I)) \times TAN (T8(I))$$

+
$$F1(I) \times W9 \times (1-R8)/(2 \times (1-W(I)/K4) \times R9 \times Cos(T8(I)))$$
 - (4-6)

66. The radius arm angle T8(I) of the Ith radius arm may be found from the suspension deflection D4(I), which will have been found as a result of the determination of W(I):

$$T8(I) = Sin^{-1} ((R9*Sin (T7) - (D4(I) - D6 - K1(K))/R9) - (4-7)$$

where D6 is defined as the suspension deflection which occurs when the radius arm angle is T7. Normally D6 is set to the deflection appropriate to a suspension load of W3/N, and T7 set to the suspension arm angle desired in the case of the vehicle standing still on level ground. The actual suspension arm angles T8(1) with the vehicle in a static condition will depend also on wheel spacings L(K), suspension settings K1(K) and CG position L(N/2 + 1), C(3).

Tracked Vehicle

- 67. The skid steering analysis developed in this document for wheeled vehicles can readily be applied to tracked vehicles, apart from the foregoing section dealing with effects of torque application at each wheel. A tracked vehicle with N road wheels is shown in Fig 9. The track/road wheel contact points can be defined by L, C coordinates as shown in Fig 2. The assumption that the whole of each wheel load is transferred onto the track/ground contact point immediately below each track/wheel contact point is consistent with the analysis being limited to vehicle behaviour on hard Thus each track behaves as a longitudinally rigid body which is in contact with the ground at N/2 points, and the theory set out in para 23 to 38 for determination of track/ground ICR is applicable. The wheel loads W(I) can be found by the method given in "derivation of: Individual Wheel Loads" para 40 to 57. The manner of application of sliding forces at the track/ground contact points is considered to modify the forces W(I) by generation of forces W2 as shown in Fig 8.
- 68. Each track has a force F3(J) applied at one end to cause sliding during skid steering. The track is assumed to be slack at the opposite 'end', immediately prior to passing below a road wheel. The track forces are given by:

$$F3(J) = \sum_{K=1}^{N} F1(I)$$

this is not equal to the total propulsive force F(J) developed by each 'track' as given by (2-6). As shown in Fig 9, F3(1) will normally be positive, F3(2) negative. In each case, a vertical force W2(I) is developed at the road wheel nearest the section of track under tension F3(J). For consistency with (4-4) both W2(I) illustrated will be negative.

69. For positive F2:

$$W2((J-1)^* N/2 + N/2) = -ABS (3(J))^* Sin (L2) - (4-8)$$

70. For negative F2:

$$W2((J-1)* N/2 + 1) = -ABS (F3(J))* Sin (Li) - (4-9)$$

all other W2 are assumed Ø.

71. W2(I) as found by (4-8) and (4-9) for tracked vehicles frequently result in negative values of W(I) implying that the road wheel in question would be raised from the ground. (The calculation of W1(I) in (4-4) assumes that the track under the road wheel is in contact with the ground). In this instance W(I) must be set to zero, as well as $\partial W1(I)/\partial D4(I)$ in equations (D-7), (D-8), (D-9) used to find chassis equilibrium. This requires suitable conditional statements in computer calculations. The reduction of wheel loads at the extremities of the vehicle in this way results in the remaining wheels carrying greater loads, but the overall effect is equivalent to shortening the wheelbase, which reduces opposition to slewing, and, generally, the values of A(J).

CALCULATION OF POWER INPUT AND DISSIPATION

Wheeled Vehicles

72. Referring to Fig 2, the N/2 contact points of a 'track' slide longitudinally (parallel to the vehicle centreline) and laterally (at right angles to the vehicle centreline) relative to the ground, at velocities V2(J) and V2(J) Tan O(I) whilst generating forces V2(I) and V2(I) respectively. (Lateral velocity in the direction of the centre of turn is defined as negative.)

The total power dissipated in longitudinal and lateral sliding is therefore, for both 'tracks':

$$N4 = \sum_{i=1}^{N} F1(i) \times V2(j) \qquad - (5-1)$$

$$N5 = -\sum_{i=1}^{N} P1(i) \times V2(j) \times Tan \Theta(i) \qquad - (5-2)$$

the power input from the vehicle transmission to the wheels is given by:

$$N6 = (2/W9) * \sum_{I=1}^{N} T2(I) * V1(J)$$
 - (5-3)

(V1(J) is the peripheral speed of the wheels relative to the hull or chassis and T2(I) is the torque input to each wheel.)

N6 normally exceeds (N4 + N5) due to power required to overcome motion resistance forces R6(I) and the additional torque required to drive the wheels due to contact patch movement.

73. T2(I) is usually negative for wheels on the 'inside' of the turn (I = N/2 + 1 to N) and this gives rise to negative power terms T2(I)* V1(J) in (5-3), when V1(J) remains positive. This represents a power input to

the vehicle transmission by the wheel. The transmission would normally be designed to 'regenerate' this power at the wheels on the outside of the turn. The sum of wheel power inputs, N6 would equal engine power input to the transmission if the transmission efficiency including the efficiency of the regenerative path within it were 100%.

Tracked Vehicles

74. Equations (5-1) and (5-2) apply to the tracked vehicle steering on hard ground which has been considered within this report. The power input to the tracks cannot be found from (5-3), however and is given by:

$$N6 - \sum_{J=1}^{2} F3(J) * V1(J)$$
 - (5-4)

or, alternatively

$$N6 = \sum_{i=1}^{N} F1(i) * V1(J)$$

OVERALL METHOD OF COMPUTATION

- 75. This section describes the essential aspects of the logic of a computer program which utilises various sections and appendices of this document in order to calculate conditions applying to a skid steered vehicle in a turn of constant radius and speed.
- 76. Figure 10 does not include every logical step in the program, but shows the essential steps. For specified values of V and R, the longitudinal ICR coordinate B determines the magnitude of the inertia forces acting at the CG, however the method used to calculate A(J) and B requires these forces as input data. Hence an initial estimate of B is required, which is used to calculate initial values of the inertia forces and a resulting calculated value of B. An outer reiterative loop is used which provides new estimates of B based upon minimisation of the error (calculated B estimated B) using a linear iteration subroutine.
- 77. The calculation of wheel loads W(I) as detailed in Para 40 to 57 takes into consideration vertical forces W2(I) which may be generated at each wheel, depending upon the specific driveline and suspension arrangements of the vehicle, and upon the torque applied to each wheel. Calculation of the wheel torques in turn depends on calculation of the ICR positions, which depends on W(I) as input data. Initial estimation of forces W2(I) is difficult and so they are initially set to zero. Wheel loads W(I) and ICR coordinates are then calculated which result in new values of W2(I). These are used as new initial estimates, the process being repeated until stable values of W2(I) are obtained. In practice this reiterative process converges fairly quickly.

PARTICULARS OF VEHICLES

78. The particulars of the vehicles are presented under the main headings TV1000, TV1333 and TV6000.

TV1000

General

79. TV1000 was a 6 x 6 test vehicle built by the UK MOD Military Vehicles and Engineering Establishment (MVEE) in order to investigate the performance of a skid steered vehicle with large wheels. Reference D contains some data on the performance of TV1000 during skid steering. The following particulars, based on TV1000, were used as input data for computer calculations of skid steering performance, and were mostly taken from Ref D.

Leading Dimensions and Mass

80. a. Number of wheels (N): 6

b. Wheelbase : 13.126 (Feet)

c. Track : 8.876 (Feet)

d. Wheel Spacings: L(1) = 6.563, L(2) = 0,

L(3) = -6.563, C(1) = 4.438,

C(2) = 4.438 (Feet)

e. CG Position : H = 3.6, C(3) = 0,

L(4) = -0.21 (Feet)

f. Weight (W4) : 46424 (1b)

g. Wheel Diameter

(effective) (D9) : 4.72 (Feet)

Suspension Characterisitics

81. The total wheel travel available on TV1000 is reported in Ref A to be adjustable in stages up to a maximum of 18 inches. The relationship between suspension force W1(I) and wheel deflection D4(I) was not given. It was assumed that the suspension geometry would have been designed to provide a 'rising' characteristic, with a maximum suspension force of magnitude 2.5* W4/N (19400 lb). The force/deflection relationship assumed is shown in Fig 11.

82. The proportion of vehicle mass carried on each wheel was measured during the course of testing TV1000 and the following average results reported in Ref D:

Front wheels: 14224 lb (7112 lb per wheel)

Centre wheels: 16464 1b (8232 1b per wheel)

Rear wheels: 15736 16 (7868 1b per wheel)

83. The wheel loads calculated by the method given in para 40 to 57 assuming a static vehicle (ie, no skid steering or inertia forces being applied) were adjusted by varying the value of CG longitudinal coordinate L(4) and the centre suspension setting K1(2). For L(4) = -0.21 feet and K1(2) = 0.8 inch, the following static wheel loads were calculated:

Front wheels:

14231 1b (7116 1b per wheel)

Centre wheels:

16477 1b (8238 1b per wheel)

Rear wheels:

15715 lb (7857 lb per wheel)

hence a value of -0.21 ft was assumed for the CG coordinate L(4), and the values assumed for KI(K) were KI(1) = 0, KI(2) = 0.8, KI(3) = 0.

Radius Arm Geometry

84. TV1000 was reported in Ref D to have 'leading' radius arms for the front wheels, and 'trailing' arms for the centre and rear wheels. In each case, the speed ratio R8 of the driveline components within the radius arms was unity. Hence Z(1) = -1, Z(2) = 1, Z(3) = 1, Z(3) = 1.

- 85. The length of the radius arms R9 was assumed to be 3.0 feet.
- 86. It was necessary also to assume a value for the angle T7, the angle at which the radius arms would sit relative to a horizontal reference plane on the vehicle chassis, when each wheel is deflected by an amount equivalent to an applied load of W4/N. An angle of T7 = -8 degrees (ie wheel hub centres nominally higher than the centres of rotation of the radius arms) was found to give the best match of calculated wheel torque figures. This is discussed in more detail below.

Friction Coefficients

87. Values for the lateral and longitudinal coefficients of friction between the wheels and the ground, M8 and M9, had to be assumed. Values of 0.8 were suggested for M8 and M9 in Ref 1 and these were tried initially. It was found necessary to decrease the value of M8 relative to M9 in order to reasonably match the steering ratio required to achieve the first gear turn radius recorded for TV1000, and to match the wheel power inputs recorded for a neutral turn. The values finally used for the calculations were M8 = 0.75, M9 = 0.85.

Rolling Resistance

88. Reference D reports an estimate of the rolling resistance of TV1000 of 1000 lb on level ground. This would lead to a value of 1000/46424 = 0.0215 for K2 in equation (5), para 28. A value of 0.02 was used for K2 in the calculations.

Tyre Contact Point Movement

89. Reference D contains the following data for TV1000 climbing directly up three slopes, with no application of stearing brakes:

Total Torque (LB-FT) To all Wheels
33107 39568 64972

- 90. To assess the extent of forward movement of the contact point of each wheel, it was assumed that each wheel provides equal propulsive force, with equal torque applied and equal movement of the contact point. In practice, the torques supplied to each wheel were not equal, particularly on the steepest slope. Equation (4-2) was then used to calculate a value of contact point movement x at each wheel for each slope value.
- 91. In this application of (4-2), (F1(1) + R6(1)) was set to W4* Sin (Slope)/N, W(1) to W4* Cos (Slope)/N and T2(1) to the torque value above, divided by N. This provides three values of x corresponding to the three slope values. These values, together with a value calculated for T2(1) = F1(1) = 0 are shown in Fig 12. The broken line shown in Fig 12 passing close to the four data points was used to obtain a value of K4 in equation (4-3) of 65400 lb.

TV1333

General

92. TV1333 is the identification of a fictitious 8 x 8 wheeled skid steered vehicle which is intended to reflect TV1000 had it been built as an 8 x 8. It was assumed that an 8 x 8 vehicle designed for the same mission as a 6 x 6 would weigh more due to the possible increase in total hull length imposed by the combination of the additional running gear, and the likely need to minimise any reduction in wheel diameter so that ground pressure is not increased.

Leading Dimensions and Mass

- 93. a. Number of wheels (N): 8
 - b. Weight : 51066 lb (A 10% weight increase was assumed)
- 94. The wheel spacings were obtained by first considering the wheel diameter. In order to keep nominal ground pressure the same as TV1000, the area of each tyre in contact with the ground per unit weight carried was made equal to TV1000. It was assumed that the contact area is proportional to diameter x section width of tyre, and that the diameter/section width ratio is not changed. Hence for a 10% total mass increase, the ratio of wheel diameters for TV1000/TV1333 is given by $\sqrt{1.1}$ x $^{6}/_{4}$ which leads to an effective wheel diameter of 4.285 feet for TV1333. The longitudinal spaces between the wheels were reduced from 1.6 feet for TV1000 to 1.0 feet for TV1333. (This results in a hull length increase of approximately 6% for TV1333, compared with TV1000). The resulting wheel

spacings were: L(1) = 7.927, L(2) = 2.642, L(3) = -2.642, L(4) = -7.927, C(1) = 4.488, C(2) = -4.488 (Feet).

95. The small increase in track compared with TV1000 is due to the decrease in section width of the tyres used for TV1333. It was assumed that the overall width of the vehicle would remain the same as TV1000. Thus:

c. Wheelbase : 15.854 (Feet)

d. Track : 8.976 (Feet)

e. CG Position : H = 3.6, C(3) = 0, L(.) = -0.25 (Feet)

Suspension Characteristics

96. The 18 inch total wheel travel of TV1000 was retained, the same general shape of suspension force/wheel travel curve retained, the force being scaled down by a factor 1.1* 6/8. All K1(K) were set = 0.

Radius Arm Geometry

97. All radius arms were made 'trailing', since it seemed likely that economy in length of driveline paths offered by front leading arms on the 6 x 6 might not be as advantageous with an 8 x 8, and that possible production cost economies resulting from a common radius arm and suspension layout might be attractive. Thus all Z(K) = 1. Radius arm length R9 was assumed to be 2.7 feet. The nominal angle T7 corresponding to radius arm position for a wheel deflection equivalent to an applied load of W4/N was set to 0° , ie the vehicle would be intended to stand on level ground in a static condition with all radius arms in a horizontal position, assuming that all wheel loads were equal.

Friction Coefficients

98. The values chosen for TV1000 were used, ie M8 = 0.75, M9 = 0.85.

Rolling Resistance

99. The value used for TV1000 was adopted, ie, K2 = 0.02.

Tyre Contact Point Movement

100. The value of K4 used was increased to reflect the small tyre size of TV1333, and consequent smaller contact point movement which might be expected to occur, K4 = 73000.

TV6000

General

101. TV6000 is the identification used for a hypothetical tracked vehicle which is intended to reflect TV1000 had it been built as a tracked vehicle, with twelve road wheels.

Leading Dimensions and Mass

102. a. Number of road Wheels (N): 12

b. Wheelbase (road wheels) : 13.126 (Feet)

c. Track : 8.876 (Feet)

d. Road wheel spacings : L(1) = 6.563, L(2) = 3.937,

L(3) = 1.312, L(4) = -1.312, L(5) = -3.937, L(6) = -6.563,C(1) = 4.438, C(2) = -4.438

(Feet)

e. CG Position : H = 3.6, C(3) = 0,

L(7) = -0.2 (Feet)

f. Weight : 46424 (1b)

g. Road Wheel Diameter : Not used in calculations for

tracked vehicle.

h. Track approach and departure angle : 30 degrees

Suspension Characteristics

103. The 18 inch wheel travel of TV1000 was retained, and suspension force, increasing linearly to a maximum of approx 2.5* W4/N (9700 lb) was assumed, as shown in Fig 13. It was found that some combinations of forces acting on the vehicle could cause individual wheels to reach full deflection, and it was necessary to model a 'bump stop'. This was done by adding an additional inch to the wheel travel in which the suspension force rises steeply from 9700 to 30000 lb. All K1(K) were set = 0.

Radius Arm Geometry

104. As detailed in para 40 to 57, the determination of wheel loads W(I) for a tracked vehicle for the calculations described in this report depends upon the track tension F3(J) and the track approach and departure angle L1 and L2, rather than the radius arm geometry and torque applied to each wheel, the latter being zero for a tracked vehicle. The calculation of radius arm position angles T8(I) was retained for reference, for this purpose the nominal setting angle T7 was made 0 and the radius arm length R9 set to 2 feet.

Friction Coefficients

105. Values of M8 = M9 = 0.8 were used, which are assumed to be consistent with the track being equipped with rubber pads for operation on hard surfaces.

Rolling Resistance

106. The rolling resistance of a tracked vehicle would be expected to be greater than for a wheeled vehicle. Ref D used a factor of 0.04 for obtained total rolling resistance of a tracked vehicle from total weight.

This was in effect adopted for the calculations within this report, ie K2 = 0.04. The method of application of K2 (via equation (5) in para 28) results in the rolling resistance generated by each track being unequal if unequal proportions of vehicle weight are carried by each track. Hence the total rolling resistance of the vehicle will always be W3* K2, with an additional moment applied to the vehicle if the rolling resistance of the tracks are unequal, resisting turning if the more heavily loaded track is on the outside of the turn.

107. Tyre Contact Point Movement - not applicable.

RESULTS OF SKID STEERING CALCULATIONS

TV1000 - Torque Input to Individual Wheels

- 108. Equation (4-3) gives the relationship assumed between forward propulsive force F1(I) at an individual wheel and torque input T2(I). For a given ICR position, F1(I) is dependent in turn on the vertical load W(I) and $\theta(I)$ as assumed in equation (2-1). Equations (4-5) and (4-6) summarise the relationship assumed between wheel load W(I) and torque input T2(I), radius arm position angle T8(I), radius arm reduction ratio R8, radius arm length R9, tractive force (F1(I) + R6(I)). For given positive tractive force and torque input, the wheel load W(I) is increased if T8(I) > 0 and/or R6 < 1. Increase in wheel load will, through the iterative process described in para 77, cause the torque input calculated for that particular wheel to be increased.
- 109. For TV1000, R8=1 and the measured wheel input torques shown in Table 1, are consistently lower in magnitude for centre wheels providing positive propulsive force (wheel No 2) compared with centre wheels providing negative propulsive force (wheel No 5). This pattern could only be reproduced in the calculations by making T8(I) < 0. The calculated figures in Table 1 were obtained for T7=-89 which made T8(I) < 0. This would imply that the normal position of the wheel centres are higher from the ground than the centres of rotation of the radius arms, an unexpected situation. At the time of writing this document, there was no other information available on the nominal radius arm position for TV1000. Acquisition of such additional data would provide a useful test for the theoretical assumptions made here.
- 110. It can be seen quickly from Table 1 that the theory gives good estimates for wheel torque input only at lower radius of turn. For fourth gear, the calculated values of wheel input torques are up to 175% greater in magnitude than the measured torques. This level of error is not, however, reflected in the calculated value of steering ratio and total wheel power input, which remain in reasonably close agreement with the measured values. The error in torque levels is considered likely to be an effect of tyre lateral flexibility, which was not considered in this analysis.

TABLE 1 - MEASURED AND CALCULATED WHEEL INPUT TORQUES FOR TV1000 (FIGURES IN PARENTHESIS INDICATE INPUT DATA FOR CALCULATIONS)

	Total Speed	Radius of Turn	Wheel Speed		Steering Matio	Power Input	TORQUE INPUT (LB-FT) TO INDIVIDUAL WHEELS						Remarks
	Ft/S		Inner	tritor	7	To Whis	1	5	3	14	5	6	i
linatured			-3.01	2.62	-0.87	148.2	8540	15470	9830	-7360	-18120	-9290	'Heutral' Gear
Calculated	(-0.237)	(-0.94)	-2,90	2.54	-0.674	152,1	10500	15101	10578	-8058	-17248	-11077	
Heasured		20.5	1,0)	3.34	3,064	67.25	10910	17400	10630	-9780	-18660	-10000	lat Gear
siculated	(2.15)	(20.5)	1.125	3.33	2.964	65.8	10925	15210	10807	-8039	-18113	-10922	
Heasured		46.58	6.73	10.11	1.502	107.0	10740	14400	10410	-9410	-14770	-8360	2nd Gear
alculated	(8.42)	(46.5)	6.517	10.35	1.583	111,2	11281	15634	10258	-8640	-17384	-10853	
licasured		73.5	11.85	15.21	1.284	115.1	10540	10160	12260	-9170	-11780	-8640	3rd Gear
alculated	(13.53)	(73.5)	11.483	15,41	1.342	118.1	11588	15851	9776	-9024	-16779	-10802	
Peasured		115.6	19.6	22.95	1,171	119.5	7608	7406	5244	-5070	-5715	-4800	4th Coar
aiculated	(21,44	(115.6)	19,18	23.23	1.211	131.7	12158	15933	8975	-9442	~15822	~10715	

Variation of Steering Ratio, Power Input and Power Dissipation with Radius of Turn

111. Figure 14 shows calculated values of steering ratio S (S is defined in para 20, equation (1-6)) for TV1000 travelling at negligible forward speed on flat ground, for a range of radii of turn, R. S increases steadily with reduction of R from large positive values, and approaches infinity as V1(2) approaches zero, or the 'inside' track become stationary with respect to the vehicle hull. Negative values of S start to occur as V1(2) becomes negative, or the 'inside' track moves forward relative to the hull. For S = -1 (tracks moving in opposite directions at equal speeds relative to the hull) the radius of turn is close to zero. S = 0 occurs when the 'outside' track speed V1(1) becomes zero and the radius of turn is about -10 ft.

Figure 15 shows the calculated effect of total speed on the relationship between S and R within a range of practical turn radii, for for V = 20 and 30 ft/sec, a lower limit to radius of turn was found to affect the calculation procedure as programmed for computer Below these limiting radii, solution to the equilibrium equations (2-10 to 2-12) was not found. The total inertia (centrifugal) force applied to the vehicle at these radii are equivalent to 0.73 and 0.78 respectively of vehicle mass. Given the friction coefficients assumed between wheels and ground, it could reasonably be expected that a limit to vehicle equilibrium would occur close to these turn radii. approaches the limiting turn radii at the higher speeds, the change in steering ratio for change in turn radius becomes zero, and in the case of V = 30, becomes negative before the limiting turn radius is reached. This suggests a regime of negative stearing stability, ie that a reduction in steering ratio could cause a decrease rather than an increase in turn radius.

- The calculated power input to the wheels for steady turns under such conditions, however, is very high and suggests that the lower limit to turn radius at a given speed would in practice be higher than those suggested by Fig 15. Fig 16 shows the total power dissipated in sliding of wheel contact points (N4 + N5) and the total power input to the wheels (N6) plotted against radius of turn R for a total speed V of 20 ft/sec, for TV1000. Practical considerations of engine power for a vehicle this size could be expected to impose a lower limit of about 40 feet radius for a steady turn at this speed.
- steering ratio S and radius of turn R for TV1333 and TV6000 (tracked). The general shape of the relationships for various forward speeds are not significantly different to those calculated for TV1000, and the limiting turn radii at the various higher speeds are nearly the same. The hypothetical tracked vehicle TV6000 requires a generally lower level of steering ratio for a given radius of turn. This is reflected in the lower values of A(J) found for the tracked vehicle, compared with the wheeled vehicles under equivalent conditions, and is consistent with the prediction in Ref 2 of a decrease in turning radius for an increase in number of wheels, for a given steering ratio and wheelbase/track (L/C) ratio. The values of A(J) calculated for TV1333 were not significantly less than for TV1000 because the L/C ratio of TV1333 was increased, to accommodate eight wheels with ground pressure equivalent to TV1000.
- The power dissipated in sliding of wheel/ground contact points 115. (N4 + N5), is dependant on the slip velocities V2(J) as given by equations (5-1) and (5-2). V2(J) are in turn proportional to A(J) as given by equation (1-9) and hence it could be expected that power dissipation of "equivalent" vehicles could be related to comparitive levels of A(J). Figures 16, 19, 20 show relationships between calculated power dissipated in wheel/track sliding (N4 + N5), calculated power input to wheels/tracks N6 (see equations (5-3) and (5-4)) for various values of turn radius R, for a total vehicle speed of 20 ft/sec. The calculated power dissipation in sliding for the tracked vehicle TV6000TR is significantly less than for the two wheeled vehicles. The power dissipation in sliding for TV1333 exceeds that for TV1000 due to the greater weight assumed for the 8 x 8 vehicle, and slightly greater levels of A(J). In all cases the power input N6 exceeds the power dissipation. This is due mainly to the work required to overcome motion resistance as defined by equation (2-5), and in the case of the wheeled vehicles, additional work done when the wheel input turques are increased by tyre contact point movement, as defined by equation (4-3). The latter assumption was applied to the wheeled vehicles oray, and is the reason for the difference (power input - power dissipated in sliding) being greater in their case than for the tracked vehicle.

Steering on Slopes

- 116. Skid steering calculations were performed for the three vehicles operating on a sloping plane as shown in Fig 21. Negligible forward speed V was assumed, making the inertia force terms (equations 1-4 and 1-5) zero, longitudinal and lateral forces at the vehicle CG resulting from components of the vehicle weight only (equations 1-10, 1-11 and 1-12).
- 117. Figure 19 shows a set of results obtained for TV1000 for a slope angle (T3) of 38°, for various heading angles (C8). For C8 below 4

degrees and greater than 43 degrees, the procedures for finding A(J) and B were not convergent. The physical interpretation of this is that the vehicle is unable to generate skid steering forces which are in equilibrium with the externally applied forces when attempting a steady turn outside of these heading angle limitations. The heading angle limitations therefore define part of an 'envelope' within which the vehicle is able to steer by skid steering, in accordance with all the assumptions made. Fig 22 shows that for G8 = 22 degrees, A(2) makes a transition from negative to positive values. This implies that the slip velocity V2(2) of the wheels on the inside of the turn makes a transition from negative to positive values (see equation 1-9), and for G8 = 22 to G8 = 43, both rows of wheels will have positive slip velocity, and hence generate positive propulsive forces.

118. By re-casting equation (1-6), it is possible to calculate R2 and hence R, for given S.

$$(R + SQR (R2 + 2 + (B*L(1) - C(3)) + 2))$$

for a steering ratio S of 3 (a typical 'first gear' value), calculated R increased from 12.4 feet to 98.8 feet as G8 increased from 4 to 43 degrees, indicating that a significant reduction in rate of turn can be expected to be associated with turns carried out at the higher limit of heading angle G8, for a slope angle of 38 degrees.

- Figure 20 summarizes the envelope within which solutions to the skid steering calculations were found to be possible for TV1000, for heading angles between 0 (parallel to slope) and 90 (straight up slope). The envelope indicates that at high values of T3 and G8, both rows of wheels or 'tracks' must develop positive slip velocities, or positive propulsive forces, which is consistent with overcoming the high longitudinal force which results from operation at high values of T3 and G8. A suitable physical explanation for the overall shape of the envelope has not been sought. It is considered likely that the large 'no-go' or 'no-steer' area between C8 = 55 and C8 = 90 results from the coulomb friction assumption of equations (2-1) and (2-2), Which fix the level of the forces developed by sliding of the wheels, irrespective of the speed of For C8 = 90, the greatest possible slope angle was found to be sliding. T3 - 13.5 degrees. At this point, the 'inner' 'track' was in negative slip, or generating negative propulsive force. The 'outer' 'track' was developing positive propulsive force to overcome that of the 'inner' 'track', together with the longitudinal component of vehicle weight implied by equation 1-12. This accounts for the smaller maximum slope for G8 = 90 than for G8 = 0.
- 120. Figures 22 and 23 show the envelope of skid steering solutions, or 'slope steerability diagrams' calculated for TV1333 and TV6000TR. The envelope shape for TV1333 is essentially similar to that of TV1000, except that the 'no-steer' area at high heading angles is marginally smaller, and the greatest possible slope for both G8 = 0 and G8 = 90 is higher. The envelope shape for TV6000TR is significantly different at high values of G8 to those of TV1333 and TV1000. For G8 = 90, the greatest possible slope angle with the inside track generating negative propulsive force was T3 = 14. Solutions were also found for G8 = 90 with the 'inside' track generating positive propulsive force at T3 = 27 and T3 = 28 indicating that the tracked vehicle might be expected to operate without limit on slopes of these angles. Calculation of the envelope, however, indicated a small 'no-go' area centred on G8 = 48, T3 = 28 which could theoretically impede

operation over a small range of heading angles. The significance of the small 'no-steer' area, which appears in a similar position on the diagrams for TV1000 and TV1333, has not been investigated further.

- 121. The ability of the tracked vehicle to operate at significantly higher slope angles when facing straight up the slope, compared with the wheeled vehicles, is attributed to the vehicle suspension characteristics and the interaction of the propulsive forces with the running gear.
- The tracked vehicle is mounted on a relatively large number of road wheels, each of which is attached to a suspension which under static conditions is required to provide a force of (vehicle mass normal to ground)/(number of road wheels) or (W3/N). For large N, suspension forces are modest compared with vehicle mass. This results in relatively low pitch stiffness, when compared with a vehicle of similar proportions supported by fewer wheels. When facing up a steep slope, the vehicle will 'sit back' on the rearmost road wheels and tend to lift the front wheels clear of the ground. If both tracks are generating positive propulsive forces, the associated track tension will tend to raise the rear road wheels, or reduce the load they carry. This will enhance the nose-up tendency and further concentrate the support of vehicle weight on fewer road wheels. This effectively 'shortens' the vehicle without affecting its width between tracks, or effectively reduces its L/C ratio. results in the vehicle being 'easier' to turn in that the moment generated by the tracks when slewing, which must be overcome by the moment generated by the difference in track propulsive forces, is reduced.
- 123. Table 2 shows the wheel loads W(I) calculated for the three vehicles considered at the extreme 'top right hand corner' of their slope steerability envelopes. The wheeled vehicles show considerable transfer of load onto the rear wheels from the front wheels, but not a significant reduction in the proportion of the total load carried at the extremities (front and rear) of the vehicles. The wheel loads calculated for the tracked vehicle, however, show the concentration of load onto the central road wheels which can be expected to improve the ability of the vehicle to turn under these conditions.

TABLE 2 - WHEEL LOADS CALCULATED FOR TV1000, TV1333 AND TV6000TR
AT EXTREMES OF SLOPE ANGLE (T3) HEADING ANGLE (G8) ENVELOPES

171000					14,133					TYGOOTR				
,	79	4143	4531		73	ea ea	ACLY	A(2)	В	73	CA	A(1)	V(5)	8
14	83			44,3	36	83			55.7	-28	90	13.01	0.12	-0.53
111	(10) (10)	Mari (I)	(16)	K(I)	MHEEL (I)	LOAD W(1)	MEET (1)	10A(5 W(15	Meel (1)	LOAD (1b)		NEEL -	(7P) 1040 ALI
	2473.9	Ę	1529	.0	1	2182.2	5	1375	3.6	1	221	.6	7	0.0
	711.4.6	5	6316	. 4	2	4478.0	6	3763	0.0	2	2031	.6	8	1142.6
	10493.0	6	9552	.8	\$	8,0569	7	5944	1.5	3	3862	.5	9	2973.4
					4	8845.9	8	810	8	4	5692	.7	10	4803.6
-								Ì		•	7523	.5	11	6634.5
Manager	-									6	1163	.8	12	4940.2

TRACK TENSIONS: COTER (F3(1)) = 16382.9 (1b) INNER (F3(2)) = 7051.9 (1b)

CONCLUSIONS

- 124. In common with the predictions of Ref A and Ref B the results of the numerical calculations indicate that wheeled vehicles require a significantly higher level of steering ratio or "track speed difference" to achieve a given radius of turn than an "equivalent" tracked vehicle. This results in a higher power requirement, generally, for skid steering of wheeled vehicles than tracked vehicles.
- 125. The relationship between steering ratio and radius of turn predicted for each vehicle under conditions of steady turning at high speeds suggest unstable steering characteristics, but this occurs under conditions where the predicted power requirements exceed the likely power output of the vehicle power plants. Given the assumptions of the numerical calculations, therefore which include relatively high values of friction coefficient for ground/vehicle frictional forces, each vehicle would be expected to steer in a stable fashion when performing steady (constant speed and radius) turns.
- The range of slope angles and slope heading angles over which the numerical calculations predict that skid steering is possible was similar for the two wheeled vehicles considered. The limiting slope angle for heading straight up the slope was significantly lower than for heading parallel with the slope. This, and the general shape of the envelope of slope and heading angles calculated, suggests that the ability of the wheeled vehicles to steer up slopes might be significantly reduced when the heading angle exceeds 50-55 degrees. This agrees with practical experience reported in Ref D and other documents, in relation to TV1000, but it must be remembered that the practical results were obtained with the vahicle on soft ground.
- 127. For the tracked vehicle, the limiting slope angle for heading straight up the slope was significantly higher than for the wheeled vehicles. The envelope of slope and heading angle calculated for the tracked vehicle included a discontinuity at slope angles below the limiting slope angle. This is attributed to the nature of the vehicle/ground friction assumption, which requires frictional forces to be developed irrespective of the speed of the tracks over the ground. It is concluded that the tracked vehicle can be expected to steer over a wider range of slope and slope heading angles than the wheeled vehicles. The higher limiting slope angle when heading straight up the slope for the tracked vehicle is attributed to the inherent atility of the suspension and running gear to modify the road wheel load distribution in a way which favours skid steering.
- 128. Experimental data, including wheel torque inputs, exist for TV1000 performing turns on hard ground at fairly low speeds (Ref D). The results of the numerical calculations performed for TV1000 under equivalent conditions are in good agreement with the measurements at small radii of turn, but at larger radii, the calculated wheel torque imput levels are too high. This is attributed to lack of suitable consideration of tyre flexibility within the numerical calculations.

RECOMMENDATIONS

- Using the method of analysis developed in this document, it would be possible to obtain an indication of the effects of various changes in vehicle dwsign upon the steering performance of wheeled and tracked skid steered vehicles on smooth hard ground. Under certain conditions, the method of analysis is subject to errors, but the results obtained can be used as comparative rather than absolute indications of steering performance. Should such additional information be required, the following features are recommended for investigation of their potential for improvement of skid steering performance of wheeled vehicles:
 - a. Radius arms (attaching wheels to chassis) which enclose driveline components with an output/input speed ratio of less than 1.
 - b. Irregular longitudinal spacing of wheel pairs, and variation in the proportion of vehicle weight carried by each wheel, the latter being introduced by deliberate variation of the force/deflection relationship of each wheel suspension.
 - c. Variation of the vehicle CG position.
- 130. The method developed for analysis of skid steering performance of wheeled vehicles on smooth hard ground does not adequately allow for the effects of tyre flexibility, and this leads to inaccurate results at large turn radii. Inclusion of tyre flexibility effects in the hard ground skid steering performance analysis is likely to be of less interest to Users than preparation of a soft ground skid steering analysis. Analysis of skid steering of wheeled vehicles on soft ground is considered unlikely to require inclusion of tyre flexibility effects, but would need to be accompanied by a tracked vehicle soft ground skid steering analysis, in order to compare wheeled and tracked vehicles.
- 131. If further development of skid steering analysis is desirable, the following topics are recommended for consideration, in the order of priority shown:
 - a. Wheeled vehicle skid steering on soft ground.
 - b. Tracked vehicle skid steering on soft ground.
 - c. Inclusion of tyre flexibility effects in the analysis of wheeled vehicle skid steering on ground.
- 132. Each of these topics could be expected to require significantly more resources to implement them than was required to complete the work reported in this document. Expenditure of such effort should be preceded by a survey of similar work which other agencies may be undertaking.

List of Annexes:

- A. Evaluation of Partial Derivative Terms Required to Define Estimates of ICR Coordinates
- B. Use of Data Fitting Procedure for Calculation of Suspension Forces and Suspension Spring Rates

- C. Evaluation of Partial Derivative Terms required to Refire Estimates of Vehicle Hull Altitude
- D. Illustrations

EVALUATION OF PARTIAL DERIVATIVE TERMS REQUIRED TO REFINE

ESTIMATES OF ICR COORDINATES

1. By inspection of equations (2-10), (2-11), (2-12):

$$\frac{\partial P2}{\partial A(1)} = \frac{\partial M(1)}{\partial A(1)} - C(1)^* \frac{\partial F(1)}{\partial A(1)} - (A1)$$

$$\frac{\partial P2}{\partial A(2)} = \frac{\partial M(2)}{\partial A(2)} - C(2)^* \frac{\partial F(2)}{\partial A(2)} - (A2)$$

$$\frac{\partial P2}{\partial B} = \frac{\partial M(1)}{\partial B} + \frac{\partial M(2)}{\partial B} - C(1)^* \frac{\partial F(1)}{\partial B} - C(2)^* \frac{\partial F(2)}{\partial B} - (A3)$$

$$\frac{\partial G2}{\partial A(1)} = \frac{\partial F(1)}{\partial A(1)} - (A4)$$

$$\frac{\partial G2}{\partial A(2)} = \frac{\partial F(2)}{\partial A(2)} - (A5)$$

$$\frac{\partial G2}{\partial B} = \frac{\partial F(1)}{\partial B} + \frac{\partial F(2)}{\partial B} - (A6)$$

$$\frac{\partial G2}{\partial A(1)} = \frac{\partial F(1)}{\partial A(1)} - (A7)$$

$$\frac{\partial R2}{\partial A(2)} = \frac{\partial P(2)}{\partial A(2)} \qquad -(A8)$$

$$\frac{\partial R2}{\partial B} = \frac{\partial P(1)}{\partial B} + \frac{\partial P(2)}{\partial B} \qquad -(A9)$$

2. In order to evaluate the right hand sides of equations A1 thru A9, expressions are required for:

$$\frac{\partial M(J)}{\partial A(J)}$$
, $\frac{\partial F(J)}{\partial A(J)}$, $\frac{\partial P(J)}{\partial A(J)}$, $\frac{\partial M(J)}{\partial B}$, $\frac{\partial F(J)}{\partial B}$, $\frac{\partial P(J)}{\partial B}$ (J = 1, 2)

From (8):

$$\frac{\partial M(J)}{\partial A(J)} = M9 \sum_{K=1}^{\frac{N}{2}} L(K) * W(I) * \frac{\partial}{\partial A(J)} (Sin \Theta(I)) - (A10)$$

From (6):

$$\frac{\partial F(J)}{\partial \Lambda(J)} = M8 \sum_{K=1}^{N} W(I)^* \frac{\partial}{\partial \Lambda(J)} (\cos \Theta(I)) \qquad - (A11)$$

From (7):

$$\frac{\partial P(J)}{\partial \Lambda(J)} = -M9 \sum_{K=1}^{N} W(I)^* \frac{\partial}{\partial \Lambda(J)}$$
 (Sin $\Theta(I)$) - (A12)

From (8):

$$\frac{\partial M(J)}{\partial B} = M9 \sum_{K=1}^{\frac{N}{2}} L(K) * W(I) * \frac{\partial}{\partial B} (Sin \Theta(I)) - (A13)$$

From (6):

$$\frac{\partial F(J)}{\partial B} = M8 \sum_{K=1}^{N} W(I) * \frac{\partial}{\partial B} (Cos \Theta(I)) - (A14)$$

From (7):

$$\frac{\partial P(J)}{\partial B} = -M9 \sum_{K=1}^{\frac{N}{2}} W(I) * \frac{\partial}{\partial B} (Sin \Theta(I)) \qquad - (A15)$$

These equations are derived by supposing that of the terms included in (2-6), (2-7), (2-8) only Sin $\Theta(I)$ and Cos $\Theta(I)$ (I = 1, N) are functions of A(1), A(2) and B.

3. Expressions for
$$\frac{\partial}{\partial A(J)}$$
 (Sin $\theta(I)$), $\frac{\partial}{\partial A(J)}$ (Cos $\theta(I)$), $\frac{\partial}{\partial B}$ (Sin $\theta(I)$)

and $\frac{\partial}{\partial B}$ (Cos $\Theta(I)$) may be found by differentiating (2-3) and (2-4):

$$\frac{-3/2}{2}$$
(Sin $\Theta(I)$)=-A(J)*(L(1))²*(L(K)-B*L(1))*((L(K)-B*L(1))²+(A(J)*L(1))²)
$$\frac{-3/2}{2}$$

$$\frac{\partial}{\partial A(J)}$$
 (Cos $\theta(I)$) = L(1)* ((L(K) - B* L(1))² + (A(J)* L(1))²)

$$-(A(J))^{2*} (L(1))^{3*} ((L(K) - B*L(1))^{2} + (A(J)*L(1))^{2})$$
 $-(A17)$

$$\frac{\partial}{\partial B} \left(\sin \Theta(I) = L(1) * (L(K) - B * L(1))^2 * ((L(K) - B * L(1))^2 + (A(J) * L(1))^2) \right)^{\frac{-3}{2}} - L(1) * ((L(K) - B * L(1))^2 + (A(J) * L(1))^2)^{\frac{-1}{2}} - (A18)$$

$$\frac{\partial}{\partial B} \left(\cos \Theta(I) = -A(J) * (L(I))^2 * (L(K) - B * L(1)) * ((L(K) - B * L(1))^2 + (A(J) * L(1))^2) \right)^{\frac{-3}{2}} - (A19)$$
Note that $\frac{\partial}{\partial B} \left(\cos \Theta(I) \right) = -\frac{\partial}{\partial A(J)} \left(\sin \Theta(I) \right)$

USE OF DATA FITTING PROCEDURE FOR CALCULATION OF SUSPENSION

FORCES AND SUSPENSION SPRING RATES

- 1. If the force/deflection characteristic of a suspension can be accurately represented by a series of straight lines, little problem should be experienced in writing a subroutine for a computer program which gives suspension force W1(I) and suspension rate $\frac{\partial W1(I)}{\partial D4(I)}$ for given D4(I).
- 2. This procedure may also be acceptable where the straight lines are a reasonable approximation to the smooth curve that some suspensions may exhibit. If greater accuracy is desired, a curve can be fitted to data selected from the suspension characteristic.
- 3. A 'cubic spline' data fitting routine supplied with volume 2 of the Maths Manual "Plot 50", supplied in support of the Tektronix 4054 computer was used for calculation of suspension forces generated by non linear suspensions. (N1 + 1) pairs of data points (W1(M), D5(M), M = 1 to (N1 + 1)) are used to generate a N1 x 4 array of coefficients C3 (J, K) (J = 1 to N1, K = 1 to 4). Then for D5(J) \leq D4(I) \leq D5 (J + 1).

$$W1(I) = C3 (J,1) + C3 (J,2) * *D4(I) - D5(J)) + C3 (J,3) * (D4(I) - D5(J))^2 + C3 (J,4) * (D4(I) - D5(J))^3$$

$$\frac{\partial W1(I)}{\partial d^4(I)} = C3 \cdot (J,2) + 2 \cdot C3 \cdot (J,3) \cdot (D^4(I) - D5(J))$$

$$\frac{\partial W1(I)}{\partial d^4(I)} + 3 \cdot C3 \cdot (J,4) \cdot (D^4(I) - (D5(J))^2$$
(I = 1 to N)

EVALUATION OF PARTIAL DERIVATIVE TERMS

REQUIRED TO REFINE ESTIMATES OF VEHICLE HULL ATTITUDE

1. It has been shown in part 4 that W(I) = W1(I) + W2(I) (I = 1 to N) and stated that during computation of W(I) by the method given in section 3, W2(I) remain constant. Hence from equations (3-3), (3-4), (3-5)

$$\frac{\partial M(J)}{\partial D\emptyset} = (2J - 3)^{*} \sum_{K=1}^{\frac{N}{2}} \frac{\partial WI(I)^{*}(C(1) - C(2))}{\partial D\emptyset} - (C-1)$$

$$\frac{\partial M(J)}{\partial D\emptyset} = \sum_{K=1}^{K} \left[\frac{\partial D\emptyset}{\partial W_1(K)} + \frac{\partial W_1(K)}{\partial W_1(K)} + \frac{\partial$$

$$\frac{N}{2} = \frac{N}{2} = \frac{3M(J)}{3T9} = \frac{N}{2} = \frac{3M(I)}{3T9} + (C(1) - C(2)) = -(C-3)$$

$$\frac{\partial MO}{\partial T9} = \sum_{K=1}^{\frac{N}{2}} \left[\frac{\partial W1(K)}{\partial T9} + \frac{\partial W1}{\partial DO} (N/2 + K) \right] * L(K) - (C-4)$$

$$\frac{\partial M(J)}{\partial G9} = (2J - 3)^{\frac{N}{2}} \sum_{K=1}^{\frac{N}{2}} \frac{\partial WI(I)^{\frac{N}{2}}}{\partial G9} (C(1) - C(2)) - (C-5)$$

$$\frac{\partial M0}{\partial G9} = \sum_{K=1}^{\infty} \left[\frac{\partial W1(K)}{\partial G9} + \frac{\partial W1}{\partial G9} (N/2 + K) \right] + L(K) - (C-6)$$

2. Using equation (3-1) to evaluate $\frac{\partial D4(I)}{\partial D0}$, $\frac{\partial D4(I)}{\partial T9}$, $\frac{\partial D4(I)}{\partial G9}$

$$\frac{\partial W1(I)}{\partial D\emptyset} = \frac{\partial W1(I)}{\partial D4(I)} \times \frac{\partial D4(I)}{\partial D\emptyset}$$

$$= \frac{3M1(I)}{3D4(I)}$$

$$= \frac{3 (S \{D4(I)\})}{3D4(I)} - (C-7)$$

$$\frac{W_1(I)}{\partial T_9} = \frac{\partial W_1(I)}{\partial D_4(I)} * \frac{\partial D_4(I)}{\partial T_9}$$

$$= \frac{\partial (S \{D_4(I)\})}{\partial D_4(I)} * L(K) * Cos (T_9) - (C-8)$$

$$\frac{\partial W_1(I)}{\partial G_9} = \frac{\partial W_1(I)}{\partial D_4(I)} * \frac{\partial D_4(I)}{\partial G_9}$$

$$= \frac{\partial (S \{D_4(I)\})}{\partial D_4(I)} * C(J) * Cos (G_9) - (C-9)$$

3. Substituting (C-7) thru (C-9) in (C-1) thru (C-6):

$$\frac{\partial M(J)}{\partial D\emptyset} = (2J - 3) * \sum_{K=1}^{N} \frac{\partial (S\{I/II(I)\})}{\partial DII(I)} * (C(1) - C(2)) - (C-10)$$

$$\frac{\partial M0}{\partial D0} = \sum_{K=1}^{N} \left[\frac{\partial (S \{D4(K)\})}{\partial D4(K)} + \frac{\partial (S \{D4(N/2 + K)\})}{\partial D4(N/2 + K)} \right] * L(K) - (C-11)$$

$$\frac{\partial M(J)}{\partial T9} = (2J - 3) * \sum_{K=1}^{\frac{N}{2}} \frac{\partial (S \{D4(I)\})}{\partial D4(I)} * (C(1) - C(2)) * L(K) * Cos (T9)$$

$$- (C-12)$$

$$\frac{\frac{N}{2}}{\frac{3}{19}} = \sum_{K=1}^{\frac{N}{2}} \left[\frac{3(S \{D4(K)\})}{\frac{3}{1}} + \frac{3(S \{D4(N/2 + K)\})}{\frac{3}{1}} \right] * L(K)^{2} * Cos (T9)$$

$$- (C-13)$$

$$\frac{\partial M(J)}{\partial G9} = (2J - 3) * \sum_{K=1}^{\frac{N}{2}} \frac{\partial (S \{D4(I)\})}{\partial D4(I)} * (C(1) - C(2)) * L(K) * Cos (G9)$$
- (C-14)

$$\frac{\frac{N}{2}}{\frac{3G9}{3G9}} = \sum_{K=1}^{\infty} \left[\frac{3(s \{D4(K)\})}{\frac{3D4(K)}{3D4(N/2 + K)}} + \frac{3(s \{D4(N/2 + K)\})}{\frac{3D4(N/2 + K)}{3D4(N/2 + K)}} \right] * L(K) * C(J) * Cos (G9)$$
- (C-15)

Equations (C-10) thru (C-15) provide values for all partial derivative terms contained in equations (3-6), (3-7), (3-8).

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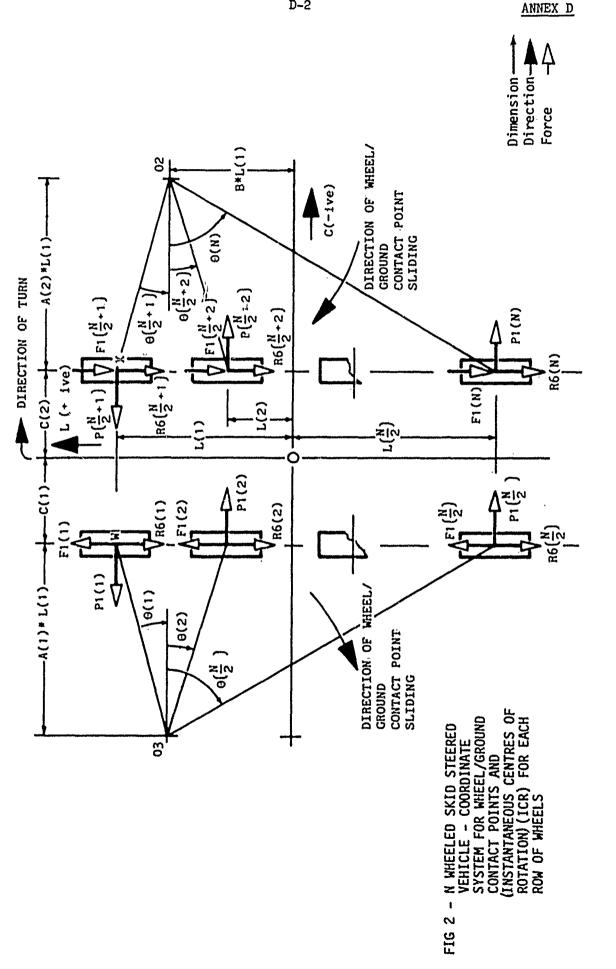
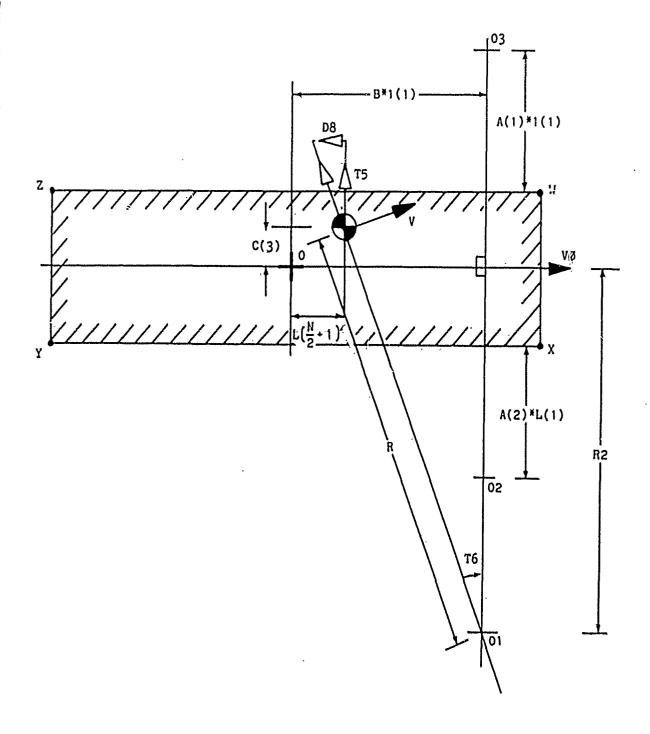
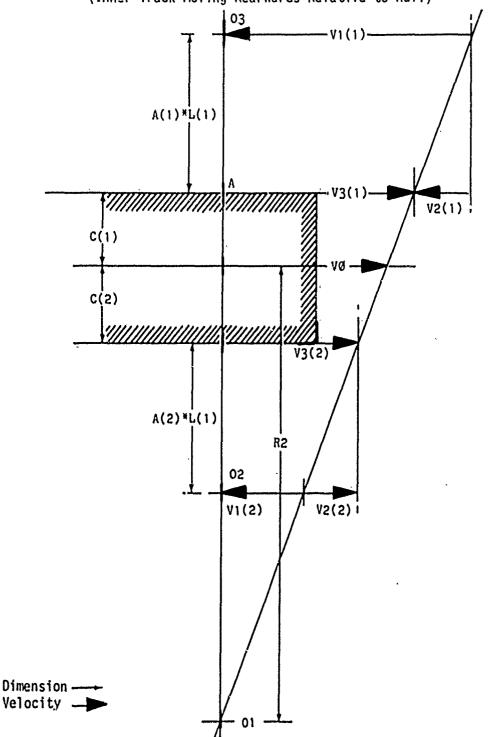


FIG 3 - TYPICAL ICR POSITIONS AND INERTIA FORCES ACTING AT VEHICLE C of G



Dimension Velocity Force

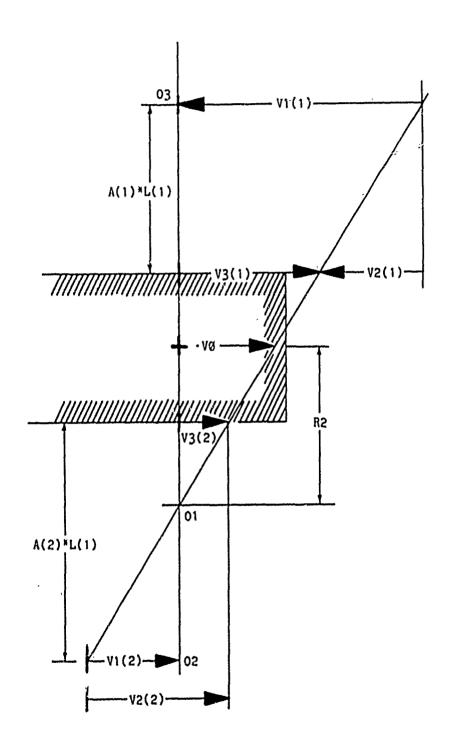
FIG 4 - VELOCITIES OF TRACKS RELATIVE TO HULL AND GROUND (Inner Track Moving Rearwards Relative to Hull)



Notes: For J = 1 (Outer), 2 (Inner), All Velocities are Resolved Parallel to Vehicle Centre Line

VØ = Velocity of Hull at Centre Line
V1(J) = Velocity of Tracks Relative to Hull
V2(J) = Velocity of Tracks Relative to Ground (Slip Velocity)
V3(J) = Velocity of Hull at Track Attachment Points

FIG 5 · VELOCITIES OF TRACKS RELATIVE TO HULL AND GROUND (Inner Track Moving Forwards Relative to Hull)



Dimension —— Velocity —

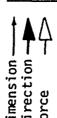
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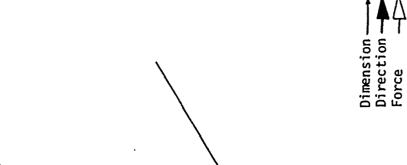
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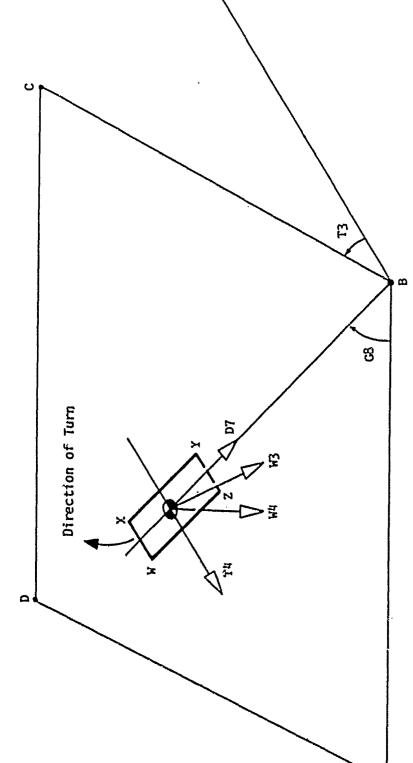
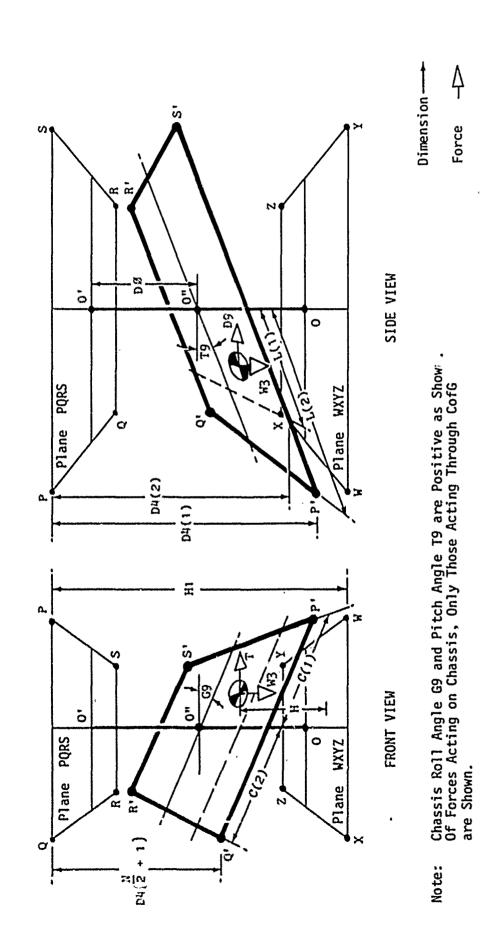


FIG 6 - OPERATION OF VEHICLE ON SLOPE - RESOLUTION OF WEIGHT

FIG 7 - SUSPENSION DEFLECTIONS AND CHASSIS ATTITUDE RESULTING FROM FORCES ACTING AT VEHICLE CofG (Unsprung Weight Assumed Zero)



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Å(£) T2(I) FIG 8 - FORCES AND TORQUES ACTING ON INDIVIDUAL WHEELS AND SUSPENSION RADIUS ARMS (Wheeled Vehicle)(Orive to Wheel Transmitted Through Radius Arm) F1(1) R6(I)-R6(I) W(I) F1(I) - R6(I)-R₃ H(I) TIN F1(I)-T8(I)

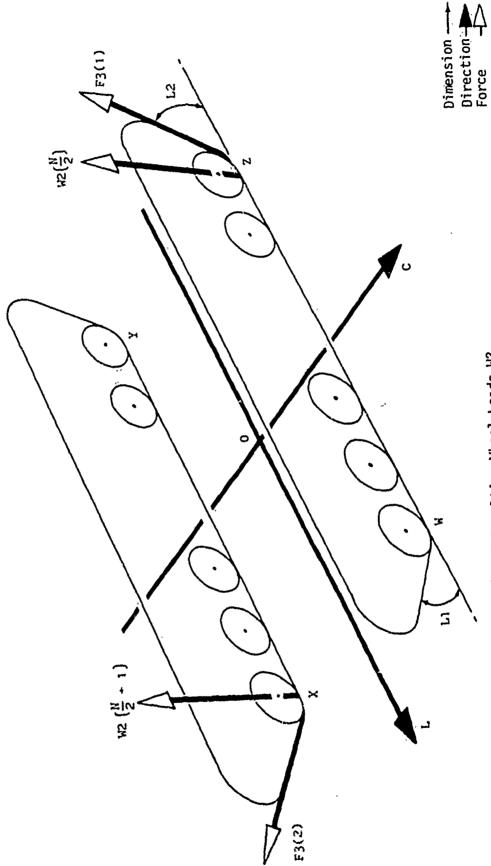
D-8

(R6(I) negative as illustrated)

Dimension — Torque /

Force





Tracked Vehicle - Track Forces F3(J) and Resulting Wheel Loads W2

ANNEX D

FIG 10 - OVERALL METHOD OF COMPUTATION

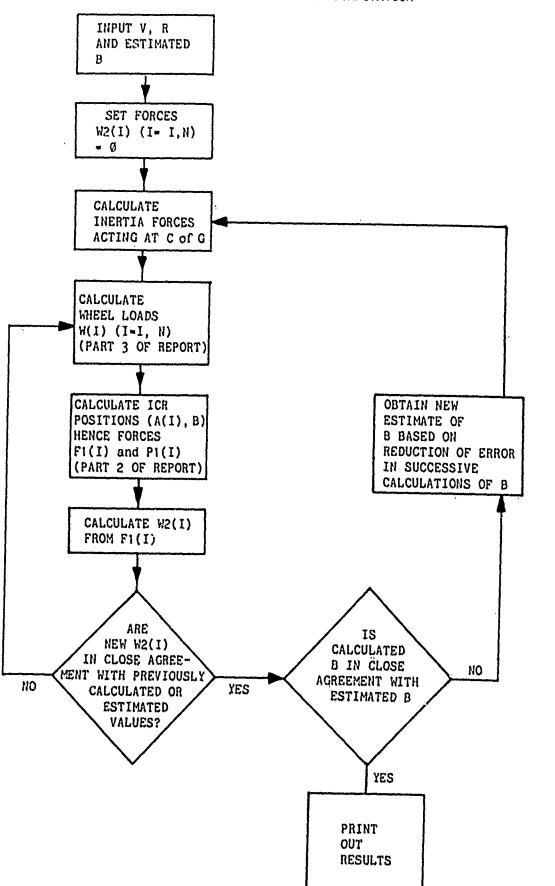
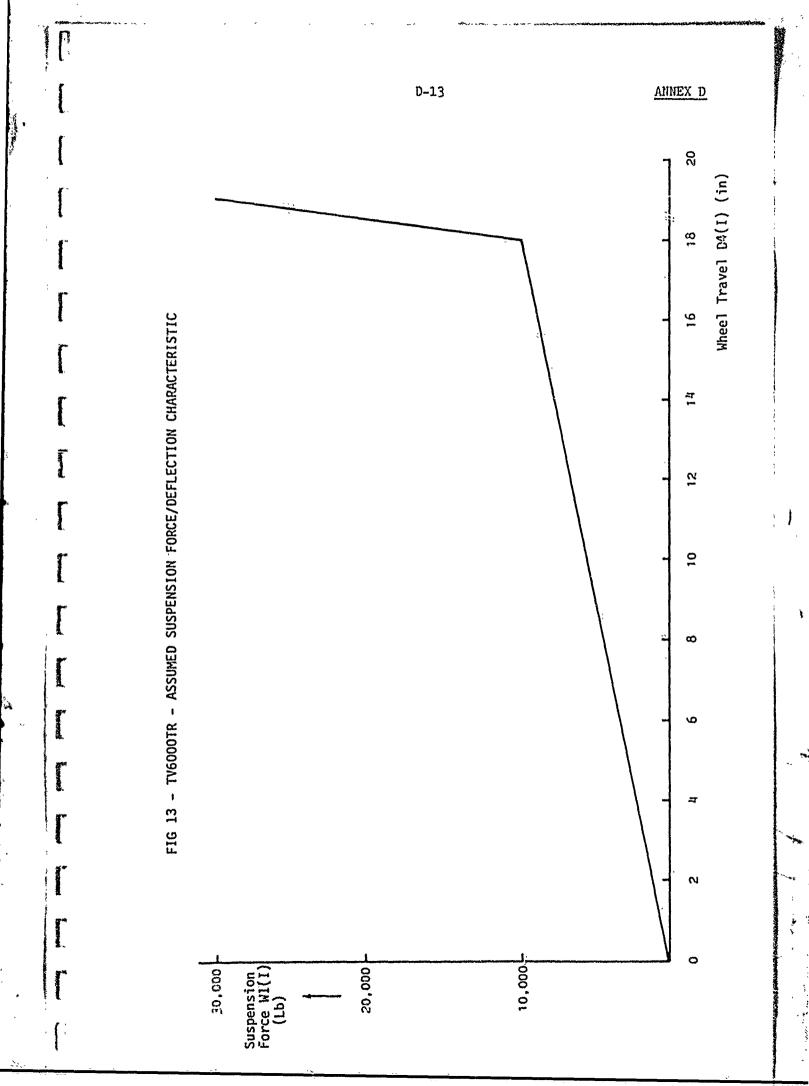
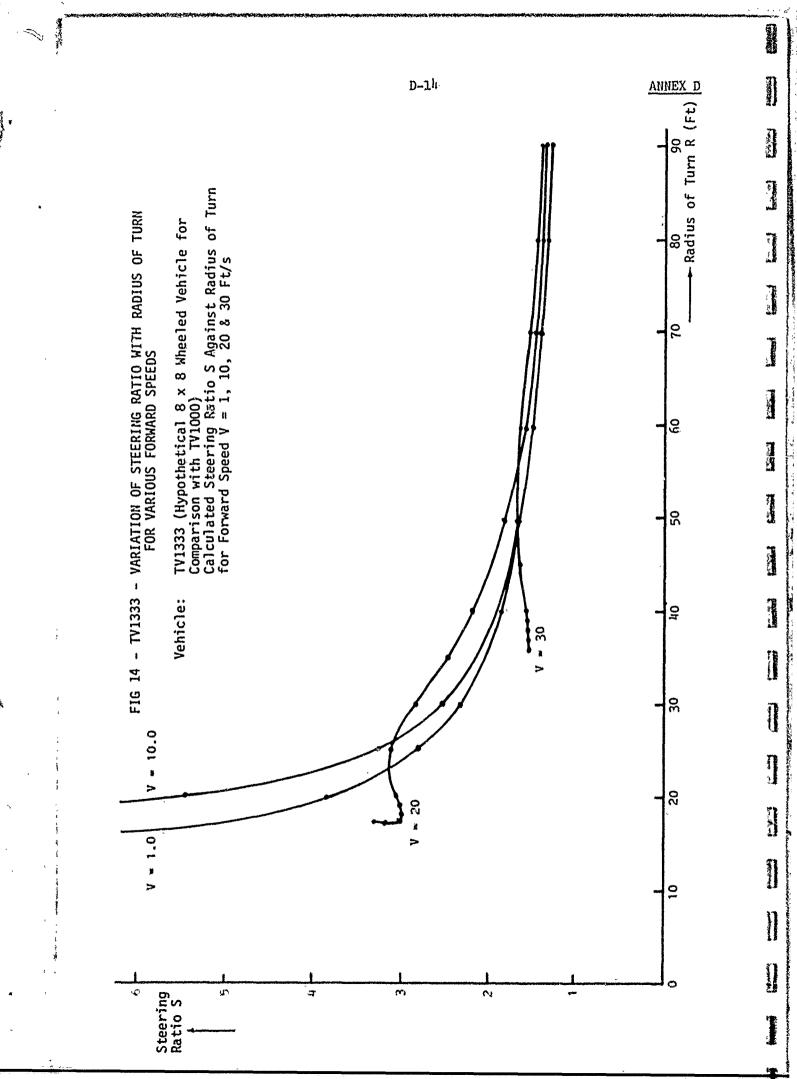


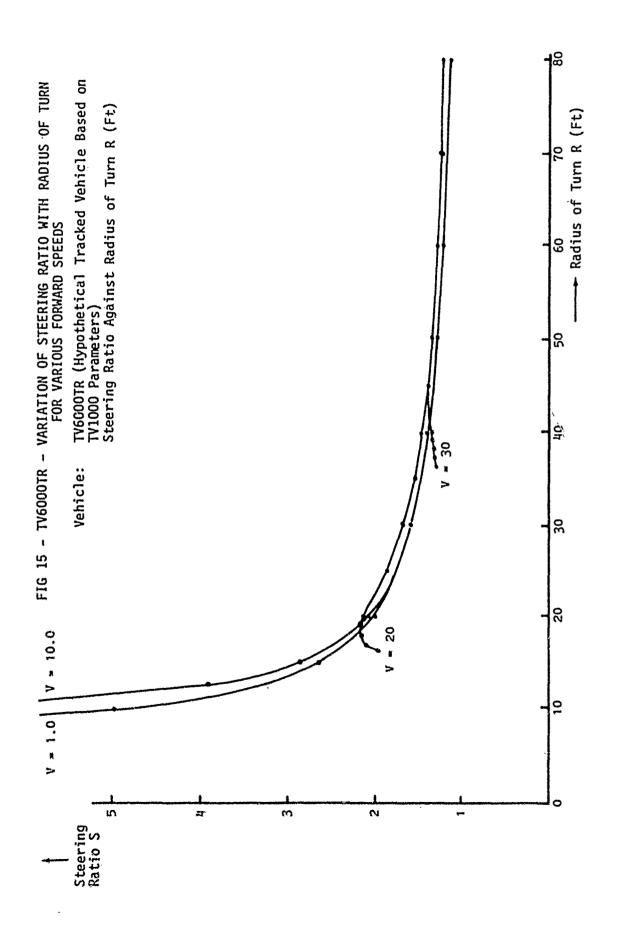
FIG 11 - TV1000 - ASSUMED SUSPENSION FORCE/DEFLECTION CHARACTERISTIC

Suspension Force (Lb)

FIG 12 - TV1000 - ESTIMATION OF WHEEL/GROUND CONTACT POINT MOVEMENT







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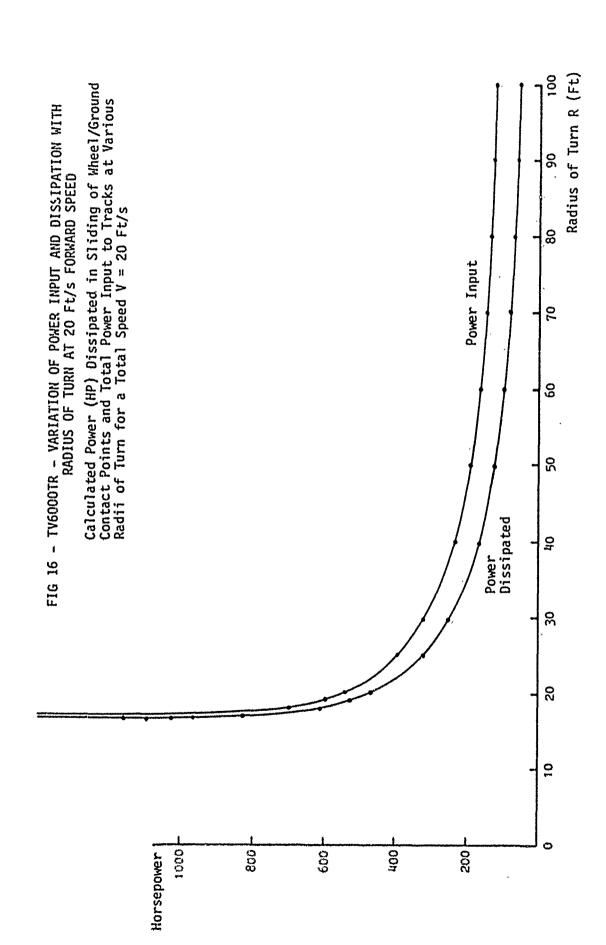
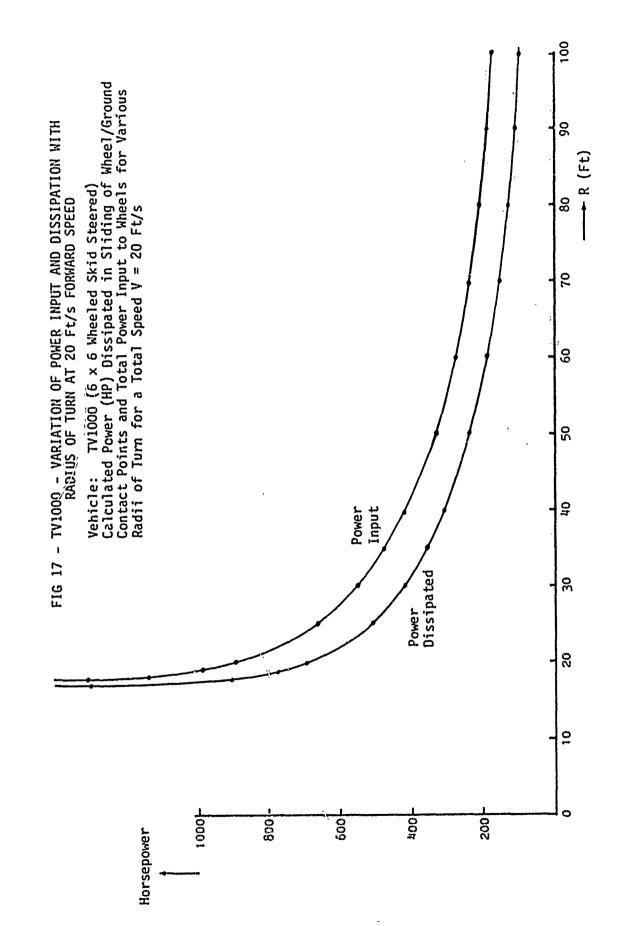
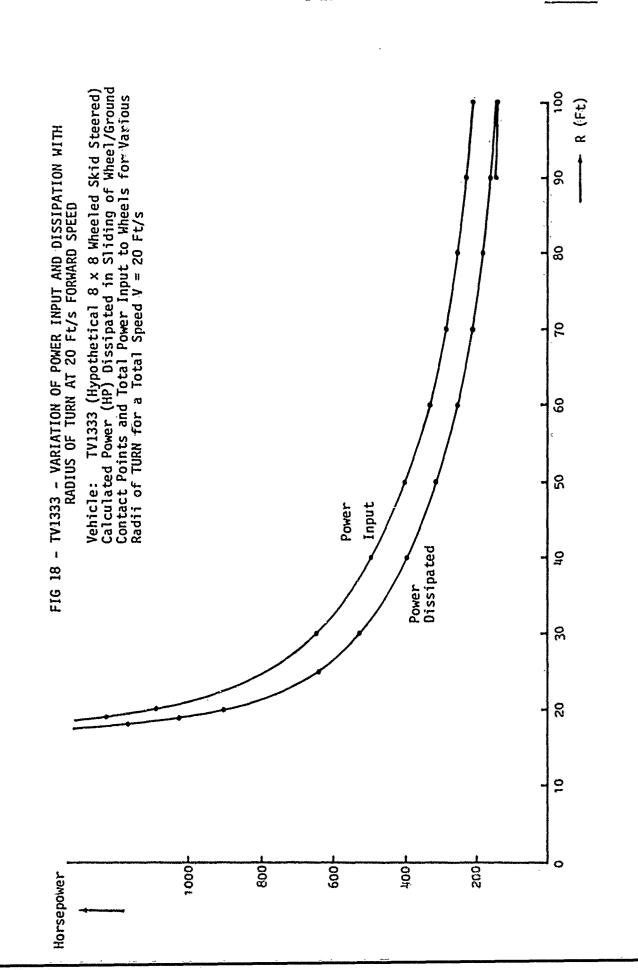
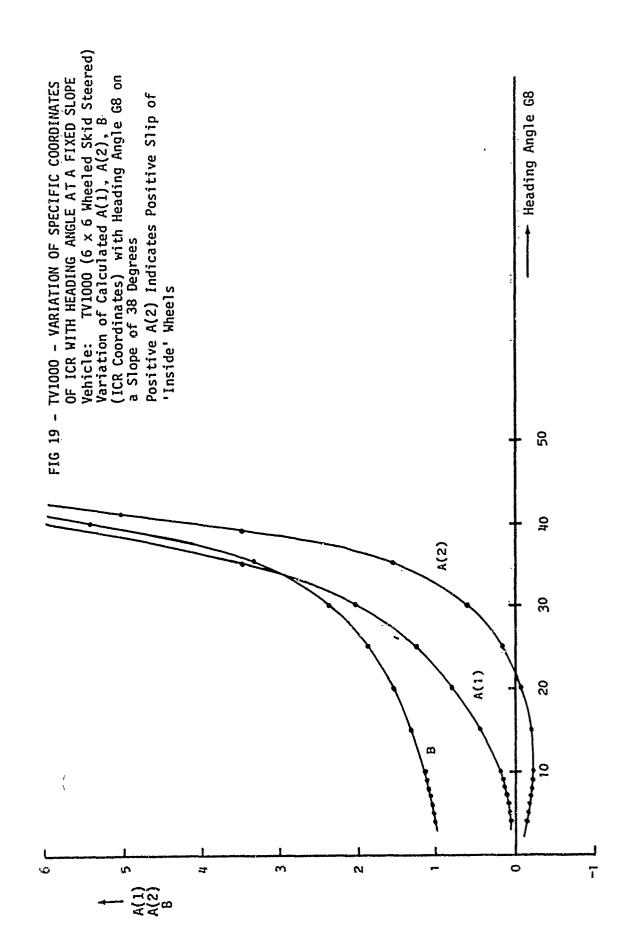


Table 1





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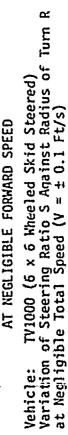
FIG 20 - TV1000 - SLOPE STEERABILITY DIAGRAM

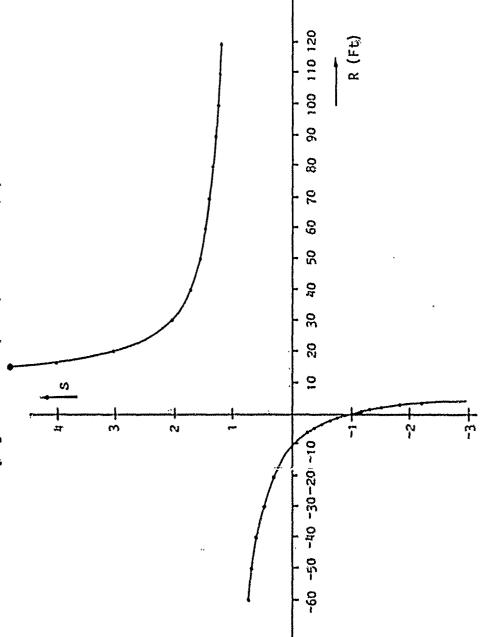
Vehicle: TV1000 (6 x 6 Wheeled Skid Steered)
Indicating Boundaries of Slope and Slope Heading Angle
for which Solutions were found for Skid Steering
Equations, with Negligible Forward Speed. Solid Line
Shows Transition from Negative to Positive Slip of
'Inside' Wheels.

Slope

FIG 21 - TV1000 - VARIATION OF STEERING RATIO WITH RADIUS OF TURN AT NECLIGIBLE FORWARD SPEED

P





The state of the s

'Inside' Track in Positive Slip

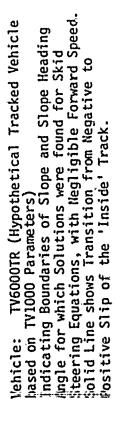
> 'Inside' Track in Negative Slip

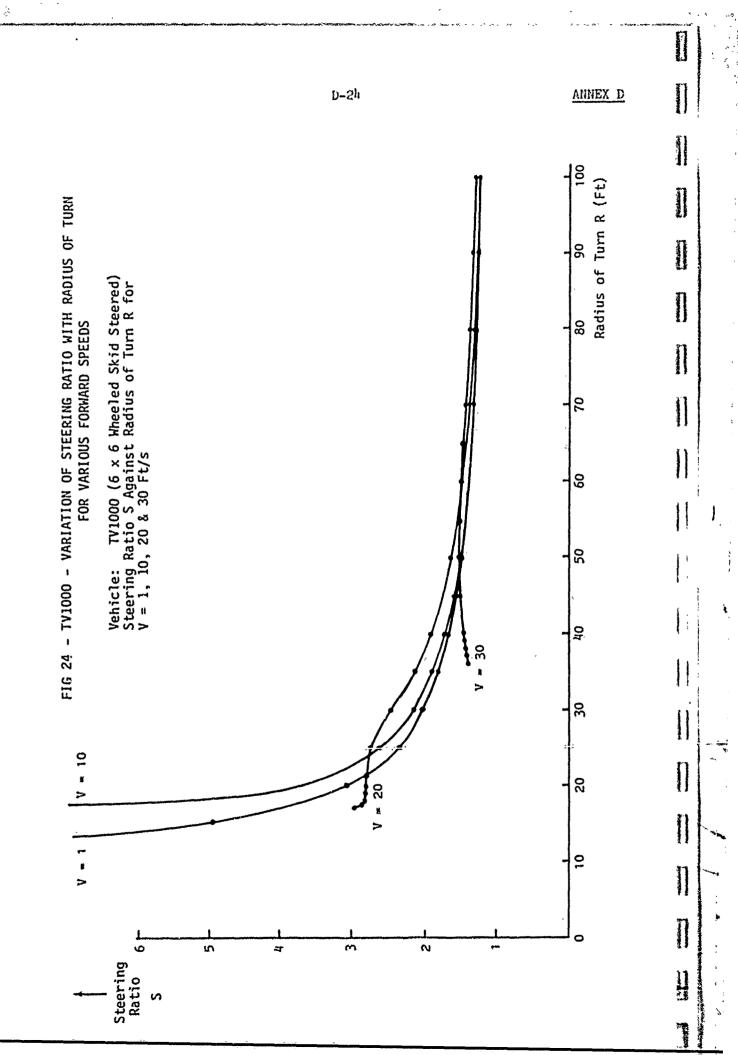
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FIG 23 - 1'V6000TR - SLOPE STEERABILITY DIAGRAM





D - 25 DOCUMENT CONTROL DATA SHEET

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16. Abstract/Summar steering of wheeled interaction of forcearried at each whe	y) Existing theoretical and tracked vehicles had es generated for skid stell of the vehicle.	ive been extended to conteering with the vertice	isider the				
calculations of ski predicted skid stee vehicle and a track	loped theory has been or d steering performance, ring performance of a 6 ed vehicle with 12 road	which has been used to x 6 wheeled vehicle, a wheels.	compare the 8 x 8 wheeled				
speed' difference a vehicle, and that t to steer over a wid wheeled vehicles.	Its indicated that the wand power input to maintant the tracked vehicle can be range of slope angles. The 8 x 8 wheeled vehicle advantage, in terms of	in a steady turn than doe expected to maintain and slope heading angles considered did not a	the tracked its ability es, than the appear to				
of the 6 x 6 vehicle indicated limitation	Its of the slope steerable, comparison of calculants to the developed the	ited results with experi ory which require furthe	mental data, or work to				

resolve. Additional keywords. Charts, Coulomb Friction,

Steering glari